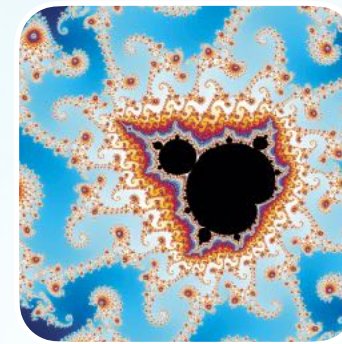




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Creativity and Storytelling in Mathematics Education

Philipp Legner, @MathigonOrg
6 May 2020



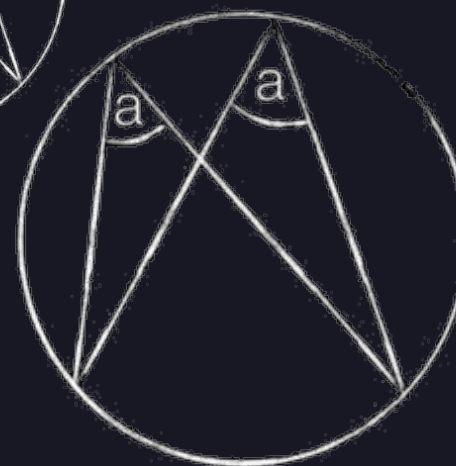
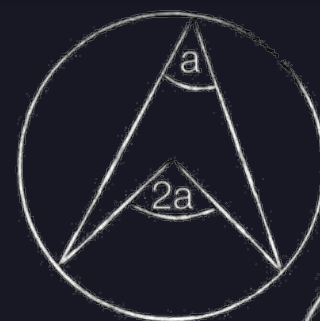
Mathigon.org



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$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



SINE RULE

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

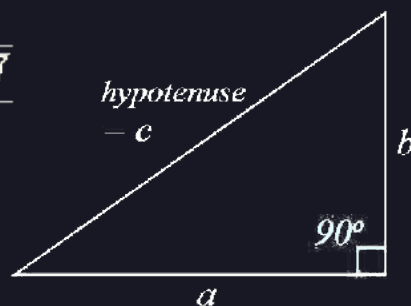
COSINE RULE

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{OR } \cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\begin{aligned} x^a \times x^b &= x^{a+b} \\ (x^a)^b &= x^{a \times b} = x^{ab} \\ x^a \div x^b &= x^{a-b} \end{aligned}$$

$$\begin{aligned} \frac{12}{\sqrt{15} - \sqrt{7}} &= \frac{12}{\sqrt{15} - \sqrt{7}} \cdot \frac{\sqrt{15} + \sqrt{7}}{\sqrt{15} + \sqrt{7}} \\ &= \frac{12\sqrt{15} + 12\sqrt{7}}{15 - 7} \\ &= \frac{12\sqrt{15} + 12\sqrt{7}}{8} \\ &= \frac{3\sqrt{15} + 3\sqrt{7}}{2} \end{aligned}$$



$$c^2 = a^2 + b^2$$



$$a + b + c = 180^\circ$$



$$a + b + c = 180^\circ$$



$$a + b + c + d = 360^\circ$$

$$\frac{d}{dx}(\sinh(x)) = \cosh(x) \frac{dx}{dx}$$

$$\frac{d}{dx}(\cosh(x)) = \sinh(x) \frac{dx}{dx}$$

$$\frac{d}{dx}(\tanh(x)) = \text{sech}^2(x) \frac{dx}{dx}$$

$$\frac{d}{dx}(\coth(x)) = -\text{csch}^2(x) \frac{dx}{dx}$$

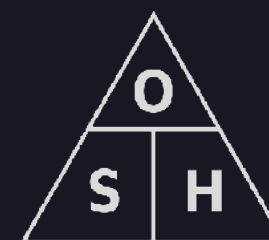
$$\frac{d}{dx}(\text{sech}(x)) = -\text{sech}(x) \tanh(x) \frac{dx}{dx}$$

$$\frac{d}{dx}(\text{csch}(x)) = -\text{csch}(x) \coth(x) \frac{dx}{dx}$$

$$\frac{d}{dx}(\sinh^{-1}(x)) = \frac{1}{\sqrt{x^2 + 1}} \frac{dx}{dx}$$

What is Mathematics all about?

SOH



sine

$$\sin = \frac{o}{h}$$

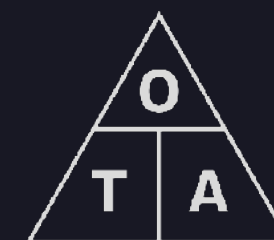
CAH



cosine

$$\cos = \frac{a}{h}$$

TOA



tangent

$$\tan = \frac{o}{a}$$

$A \cup B$: "A union B" i.e. A or B or both

$A \cap B$: "A intersection B" i.e. both A and B



What is Mathematics all about?

Meaningful Mathematics

Art and Beauty

*History of
Mathematics*

*Puzzles, Patterns
and Games*

*Understanding
Nature and Science*

Fiction

Useful Mathematics

Problem-solving

Critical Thinking

Creativity

Abstraction

Precision

Applications

Arithmetic + Algebra

Modelling + Simulation

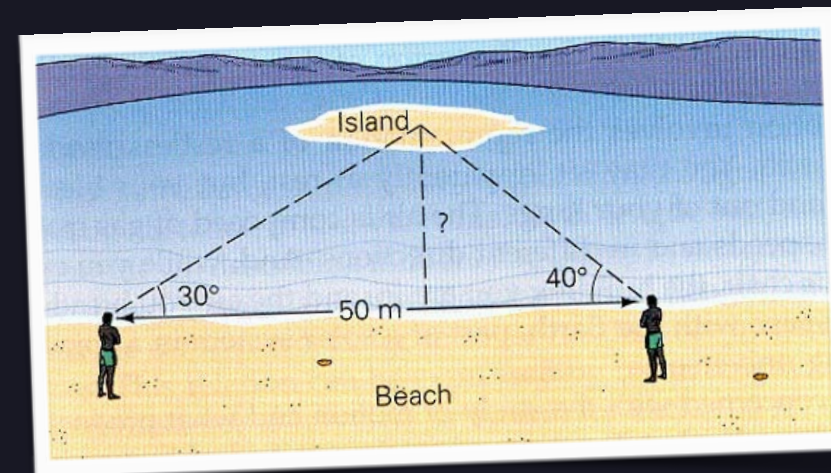
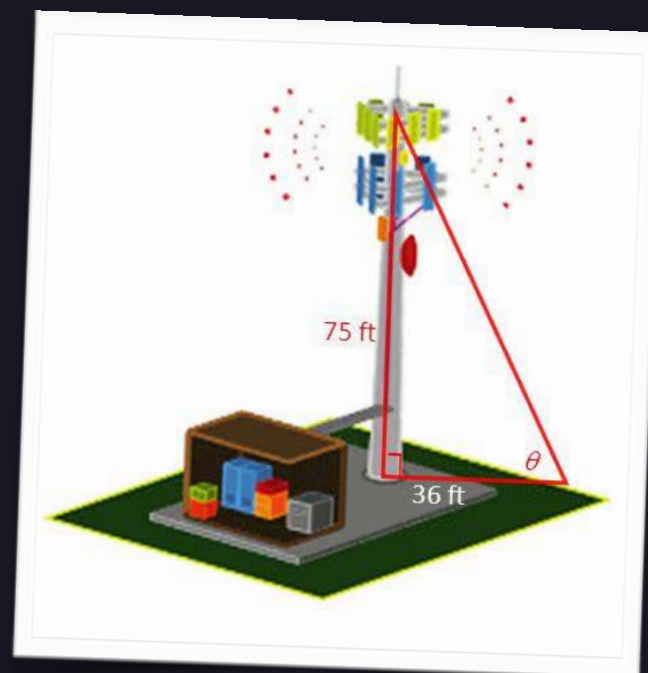
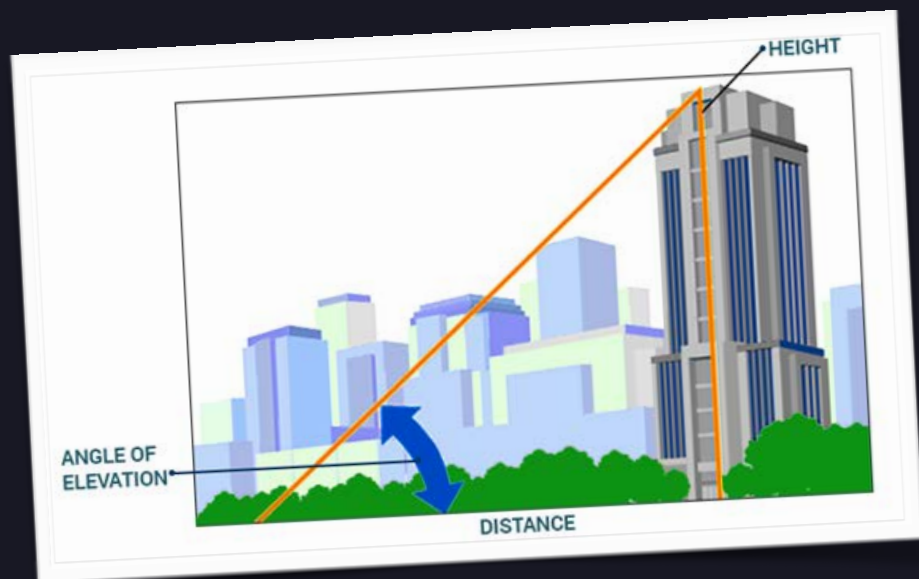
Data Science

Cryptography

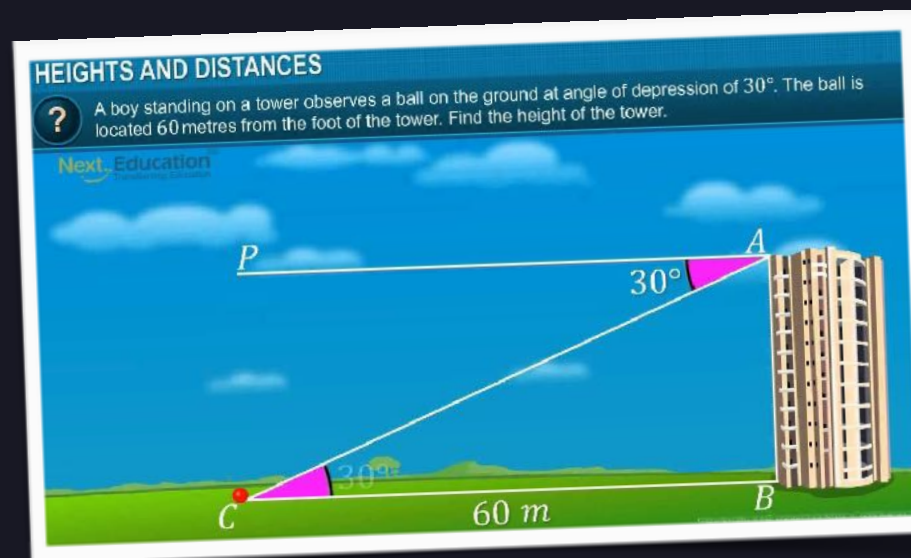
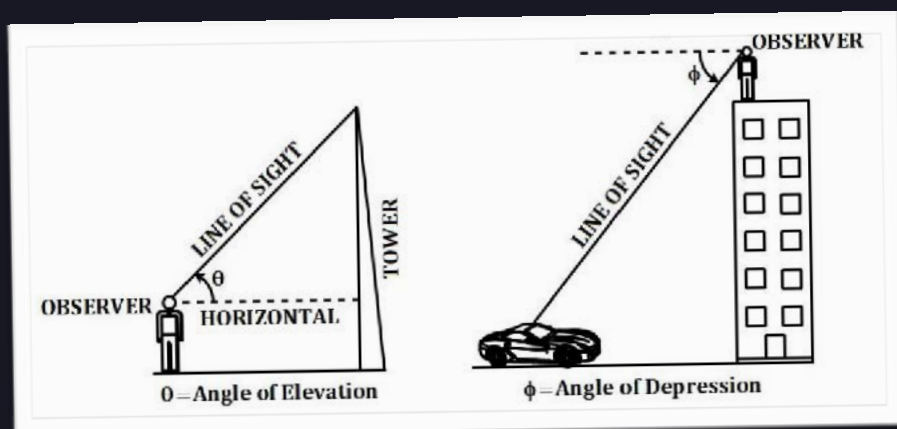
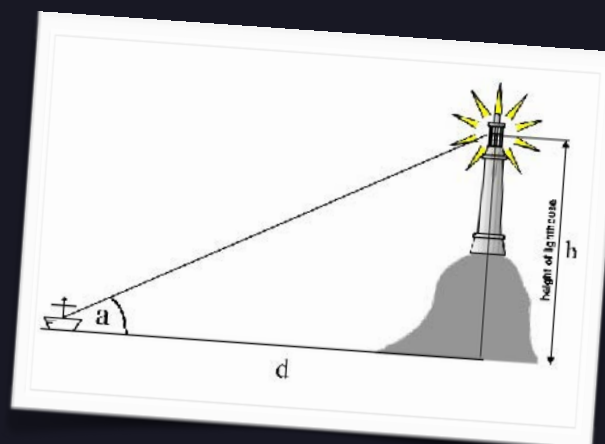
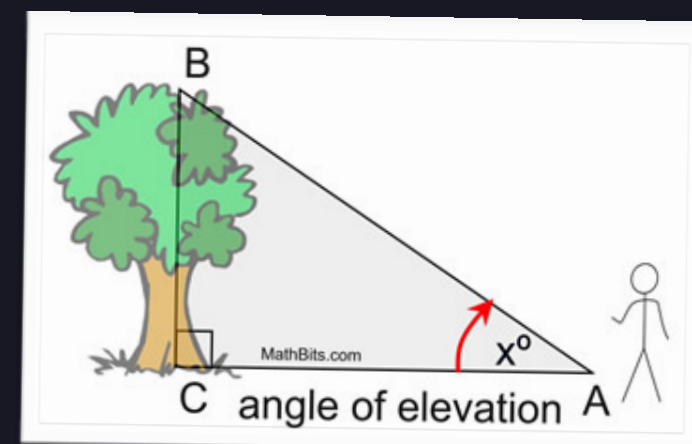


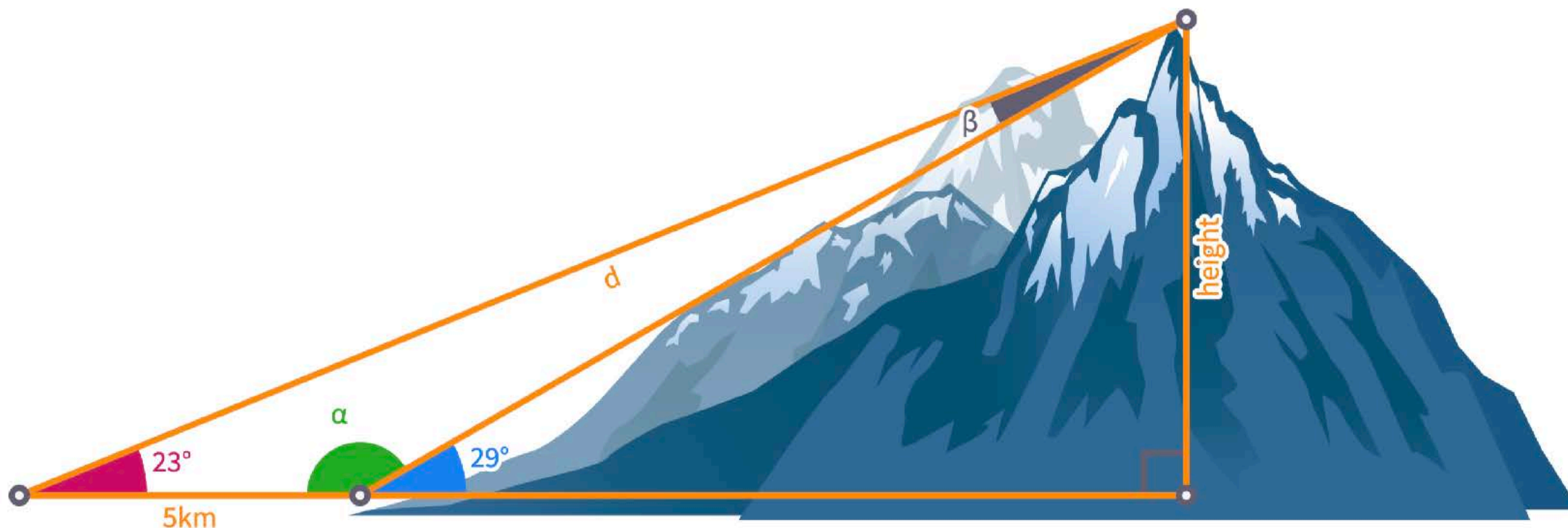
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Storytelling



Trigonometry





$$\frac{\sin 151^\circ}{d} = \frac{\sin 6^\circ}{5}$$

Trigonometry



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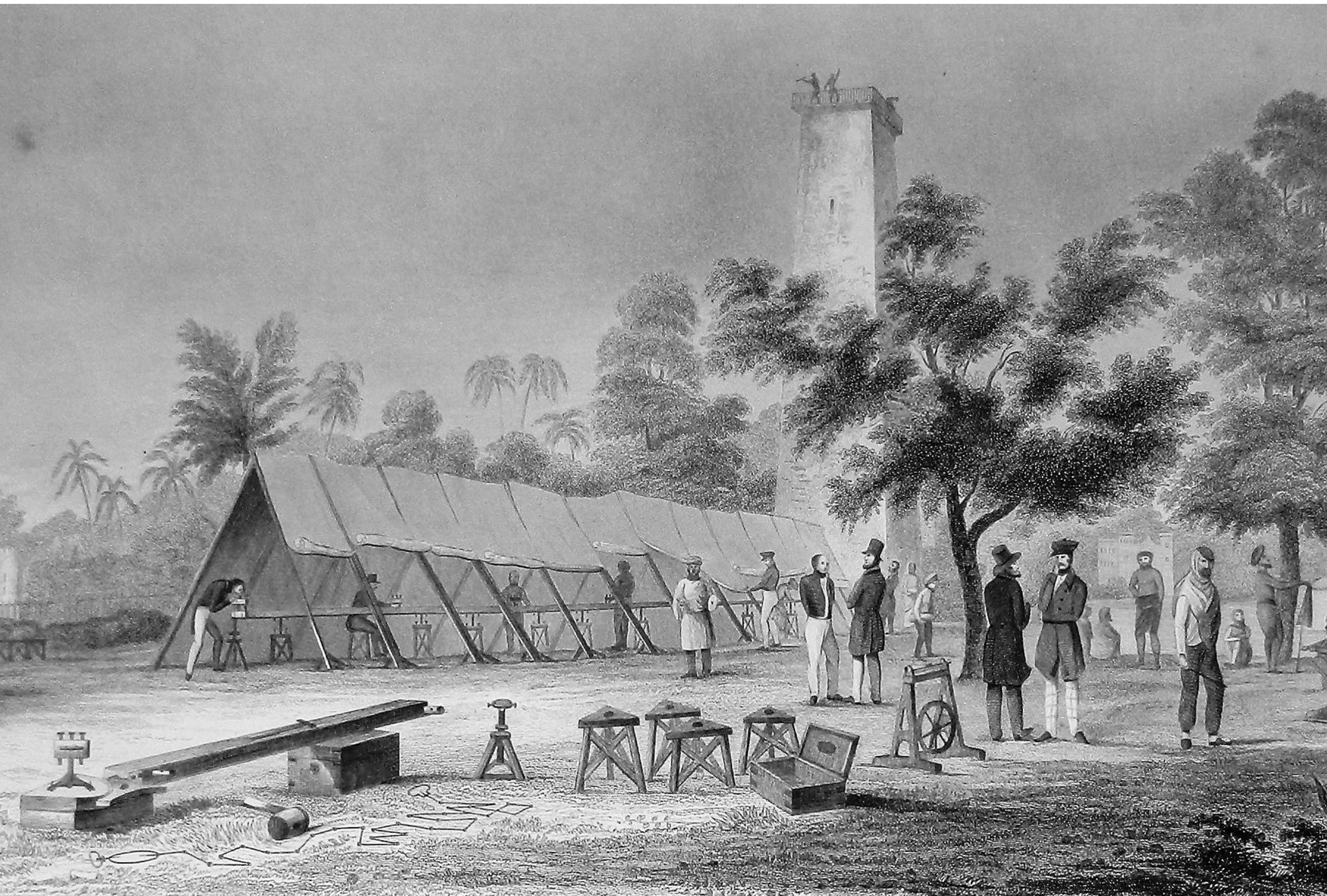


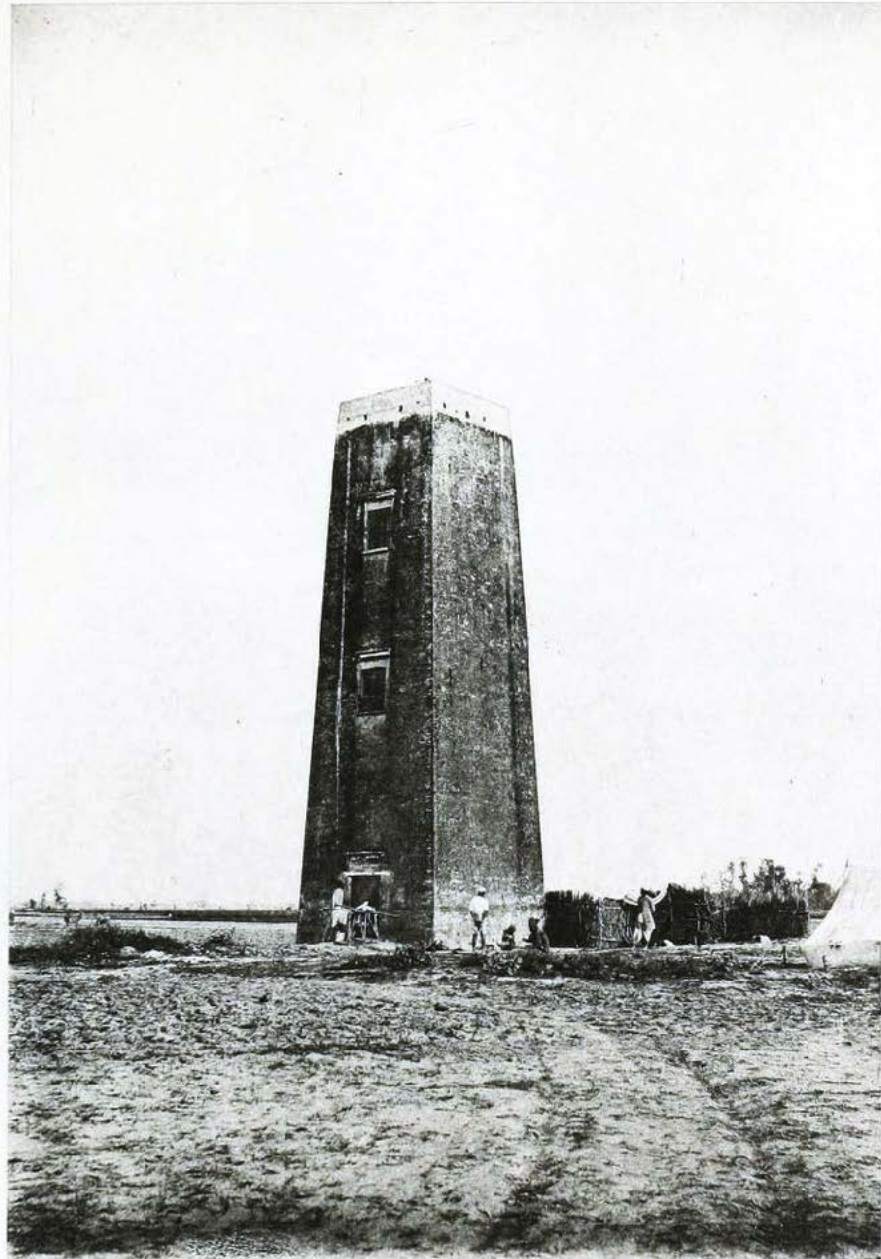
Mount Everest





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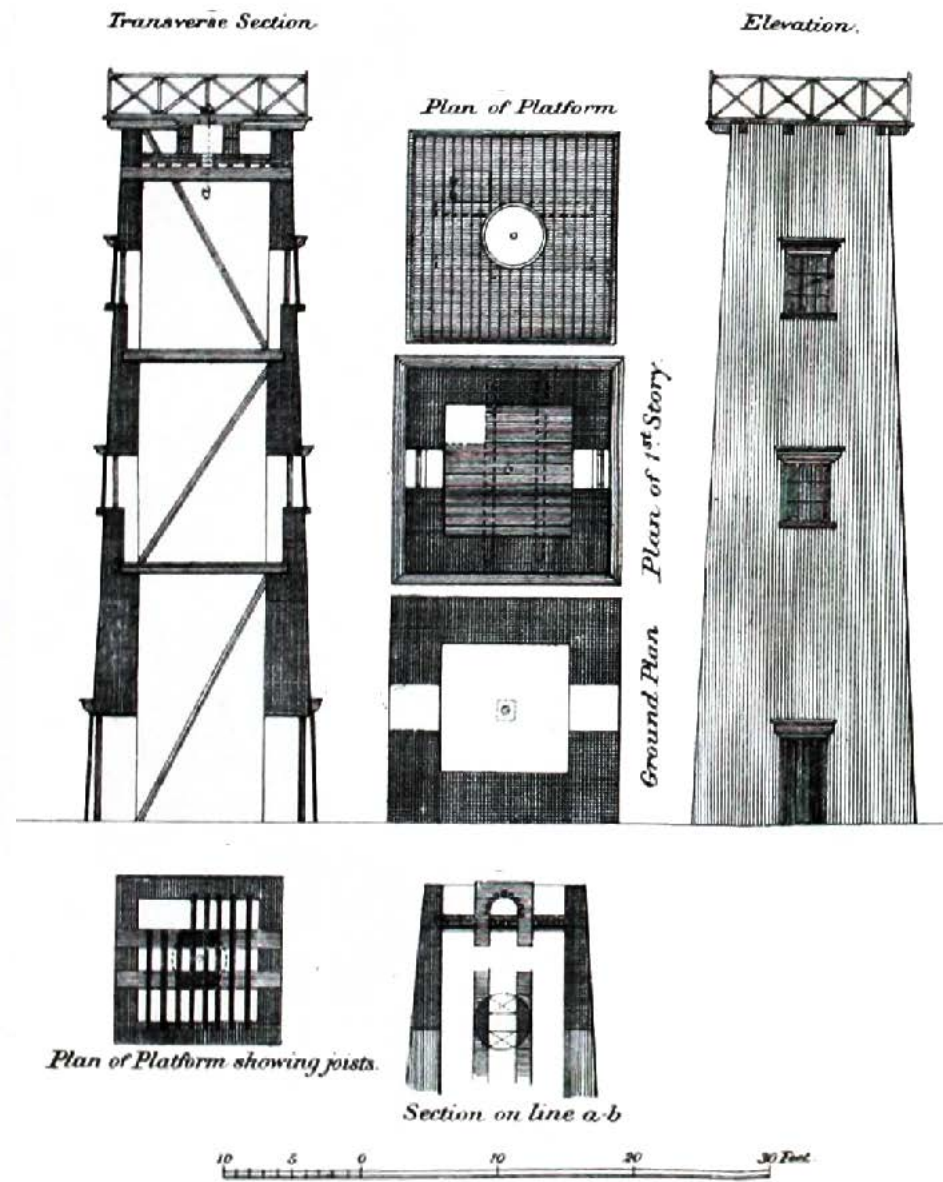
Photogravure

Survey of India Offices, Calcutta, December, 1906.

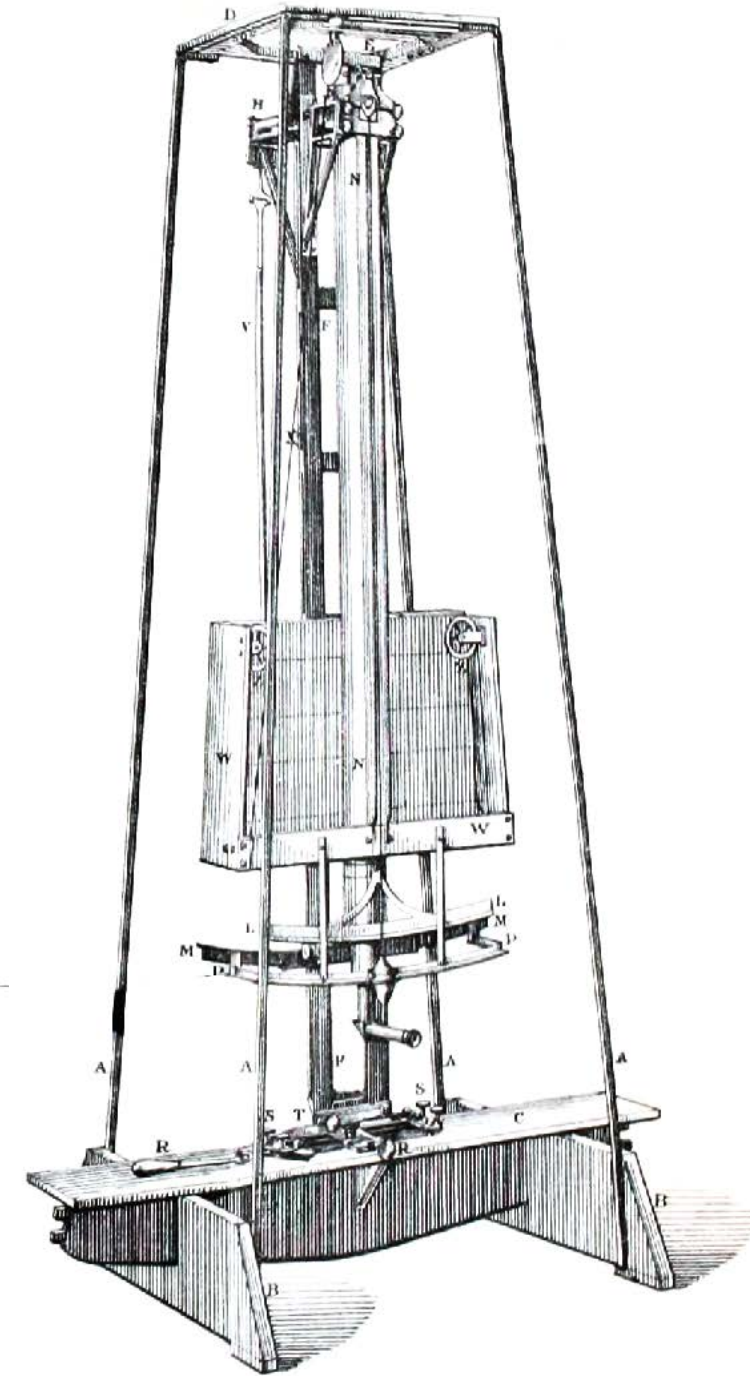
NOJLI TOWER.

A STATION OF THE GREAT TRIGONOMETRICAL SURVEY, BUILT IN THE PLAINS OF UPPER INDIA NEAR ROCKREE,
AND FROM WHICH THE HIMALAYAN PEAKS OF BADRINATH, KEDARNATH, JAONLI AND BANDARPUNCH HAVE BEEN OBSERVED
FROM A PHOTO BY C.C. SIMONS.

ELEVATION, SECTIONS & PLANS. *Illustrative of Colonel Everest's Towers on the Great Arc.*

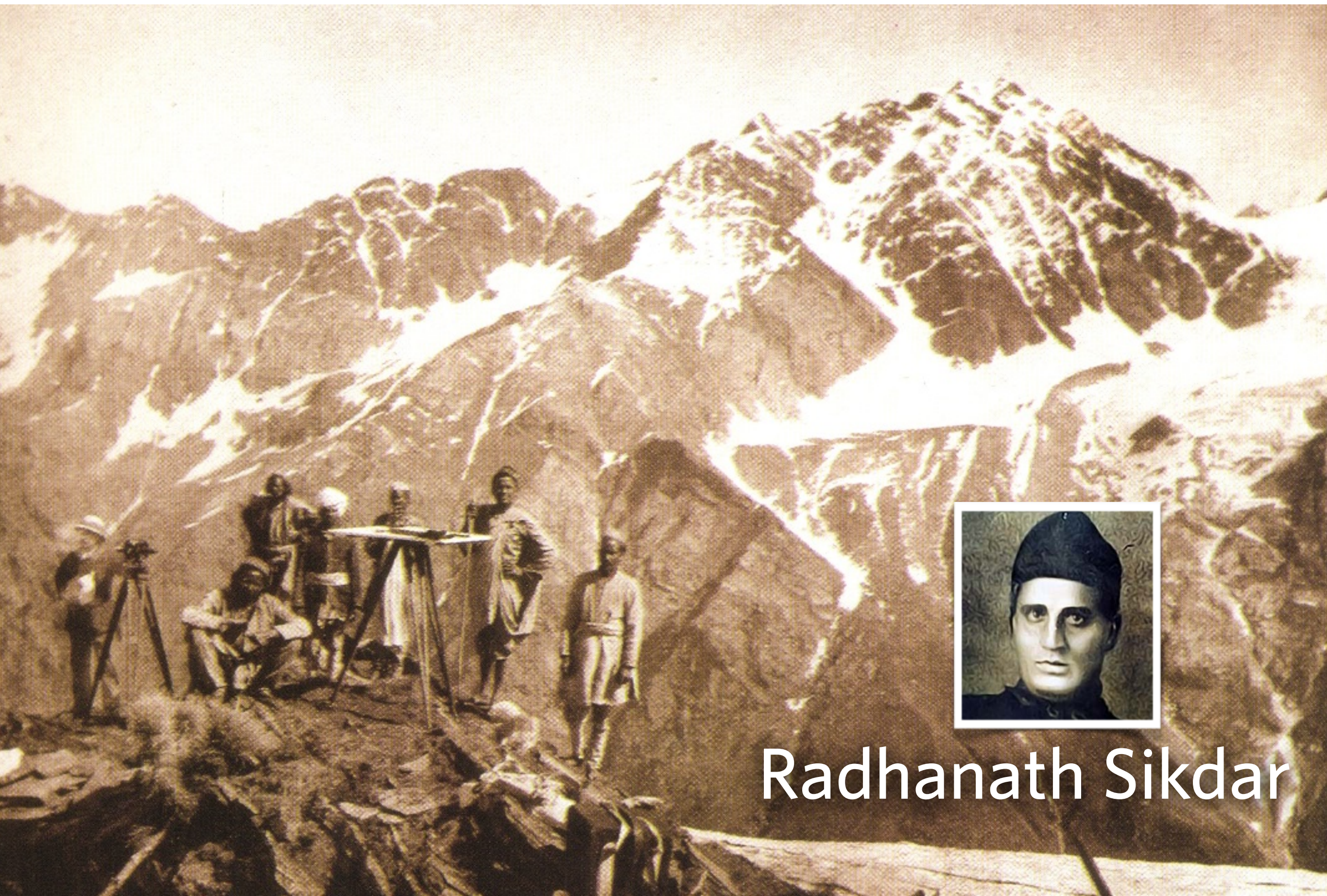


OLD ZENITH SECTOR, (RAMSDEN'S)





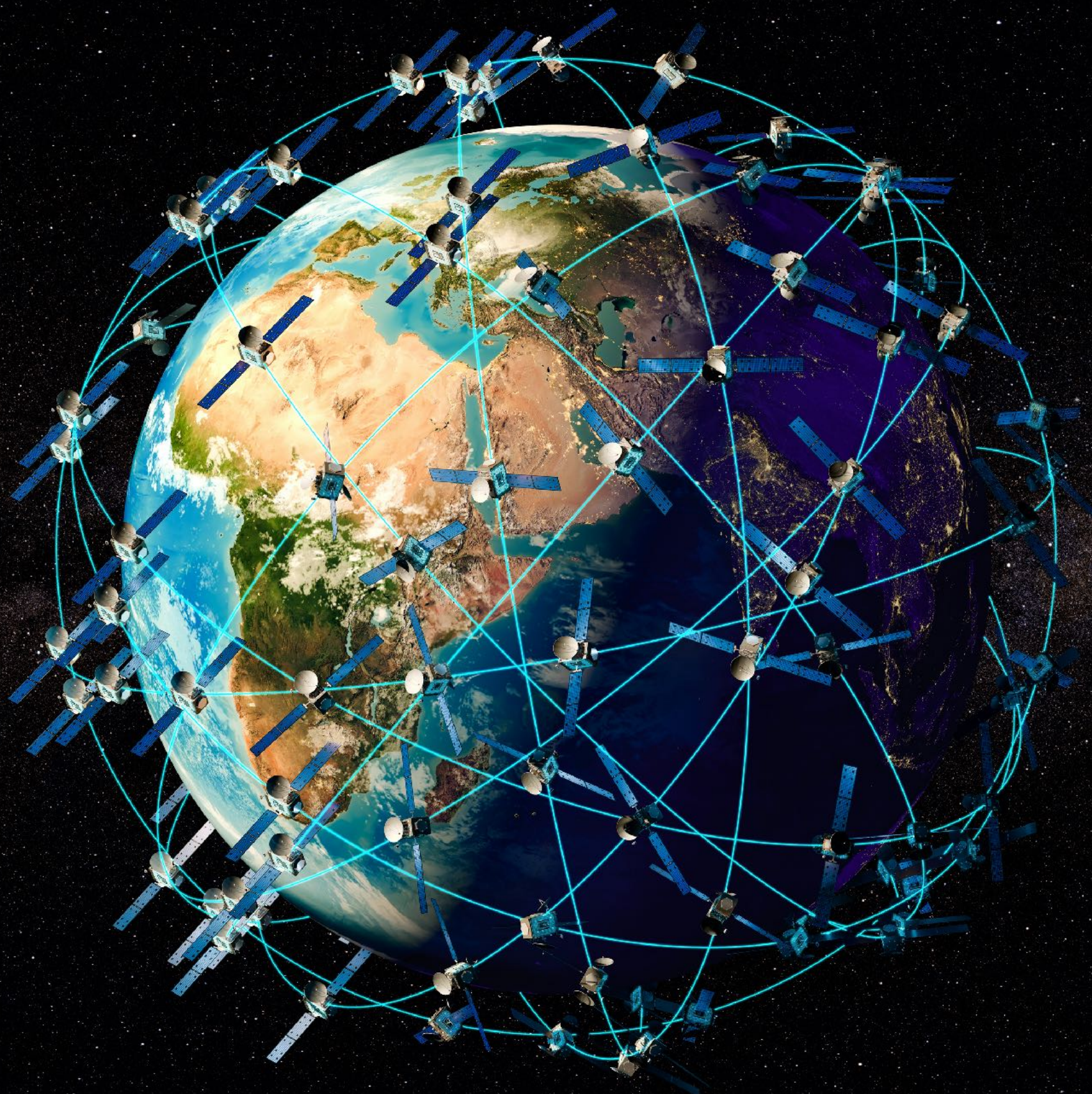
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Radhanath Sikdar



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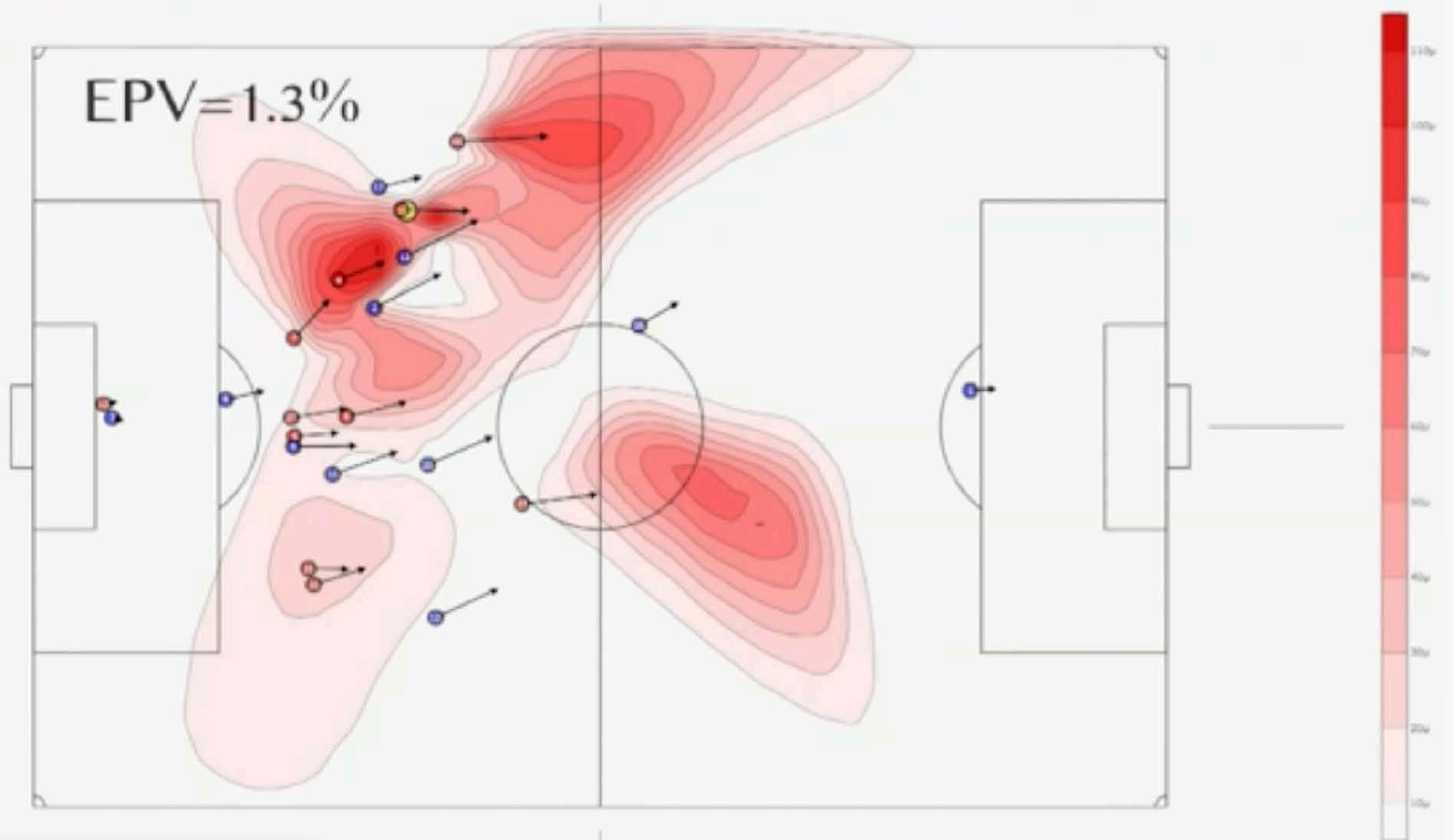


GPS



Sports Brackets





Football

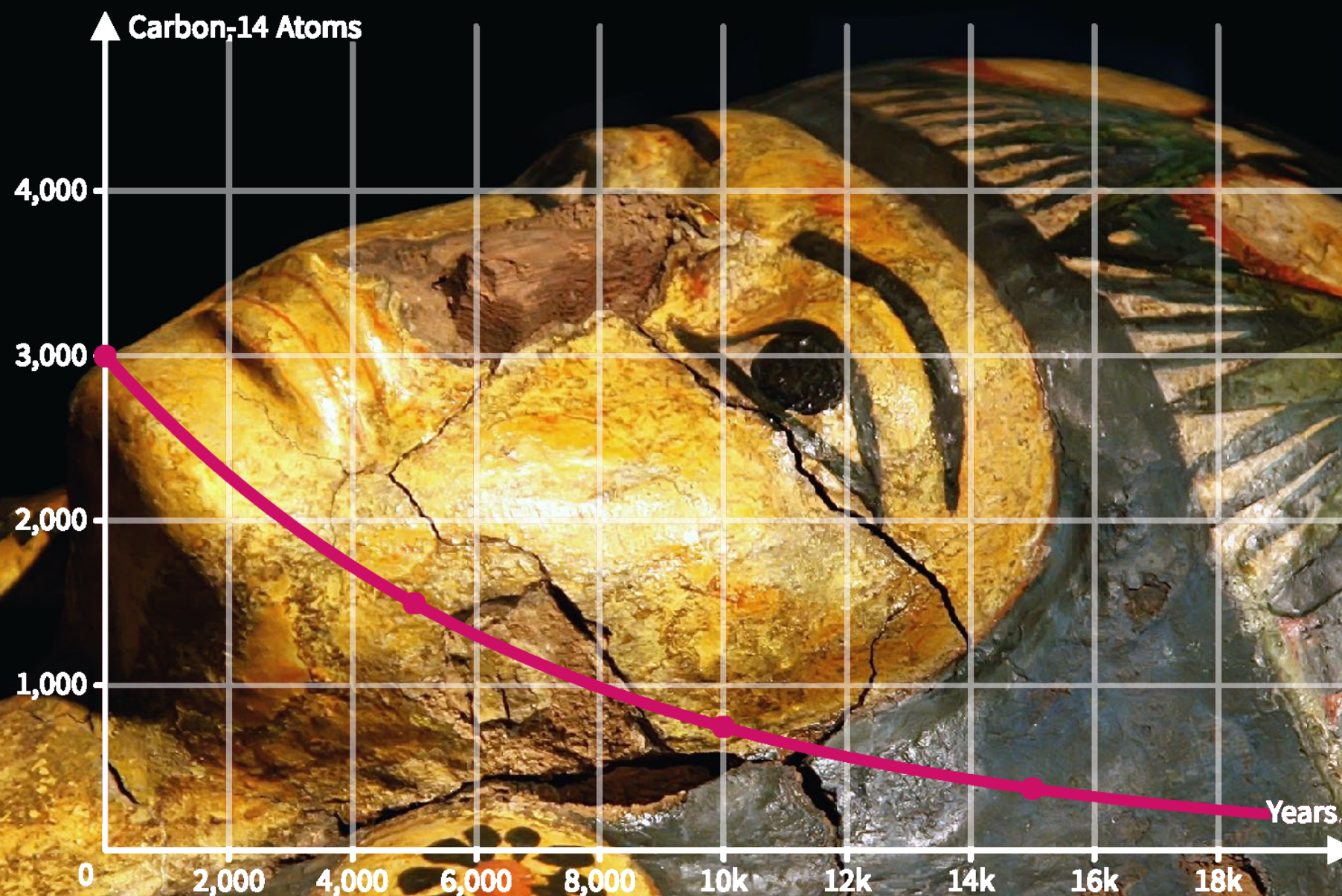


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mathigon.org/go/carbon



Carbon Dating



Carbon-14
6 protons
8 neutrons



Nitrogen
7 protons
7 neutrons



Antineutrino



Electron

Carbon Dating

A close-up photograph of a cicada on a green leaf. The cicada's wings are spread, showing intricate patterns of veins and colors. Two semi-transparent circles are overlaid on the image: a green one on the left containing the number 13, and an orange one on the right containing the number 17. The background is a soft-focus green, suggesting a natural outdoor setting.

13

17

Cicadas



<https://mathigon.org/>

13, 17

Public Key
221



Alice



Bob

Public Key Cryptography



Position



Velocity



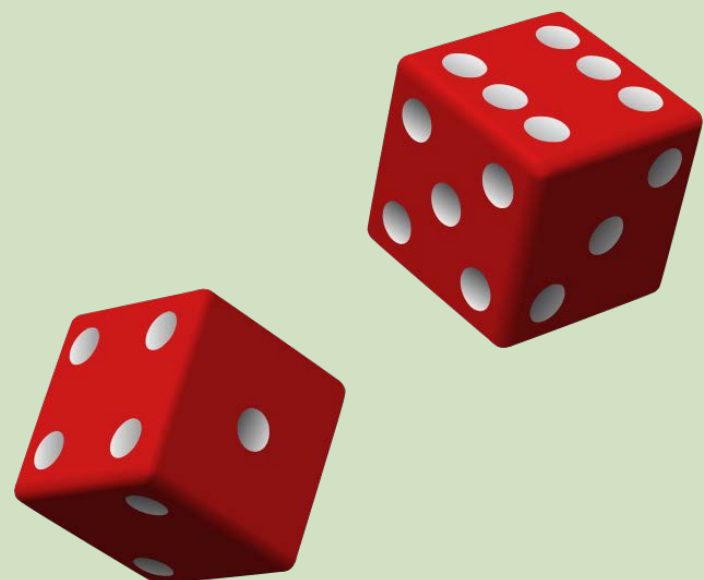
Acceleration



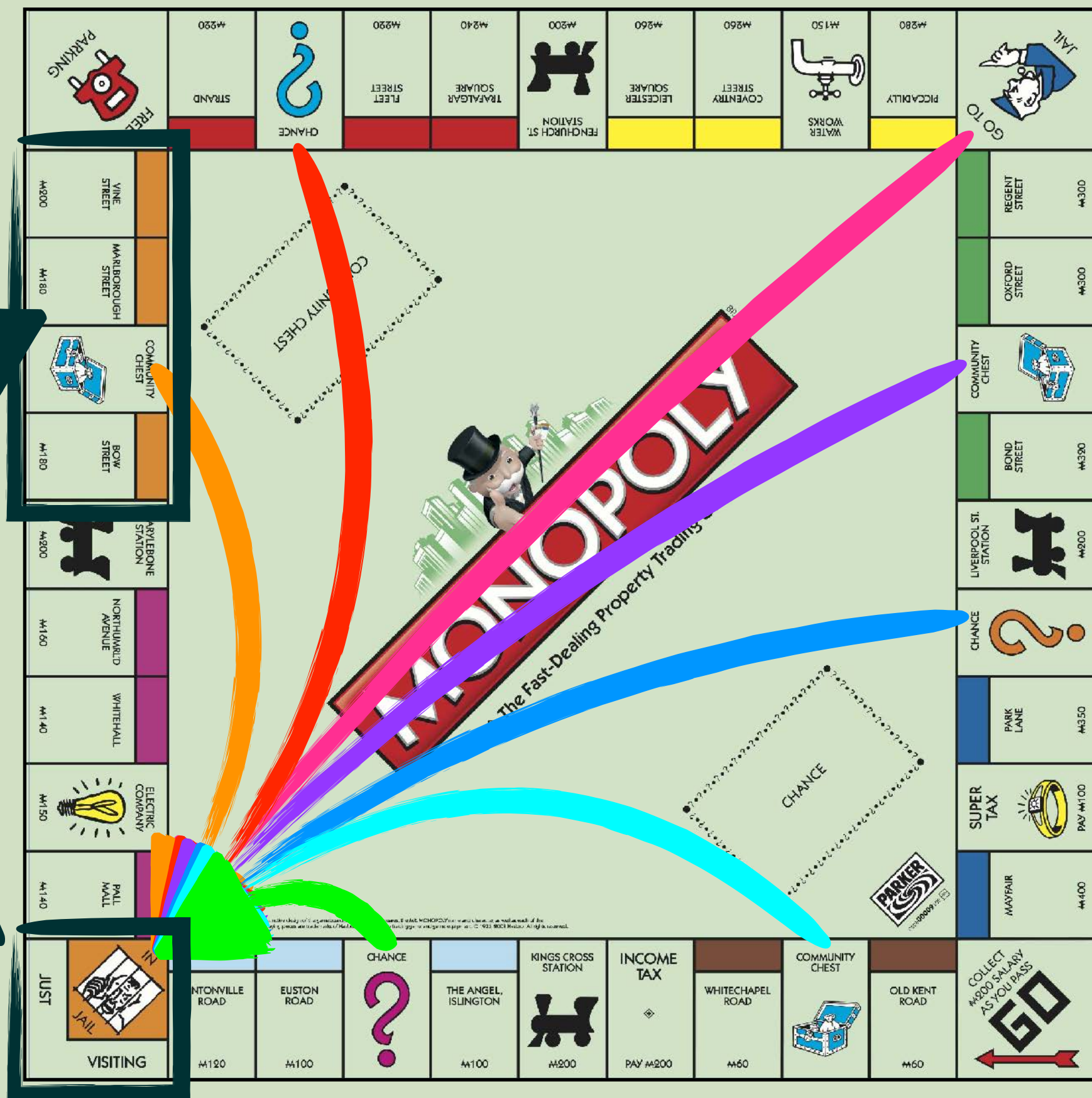
Jerk



Roller Coasters



Monopoly





2	3	4	5	6	7	8	9	10	11	12



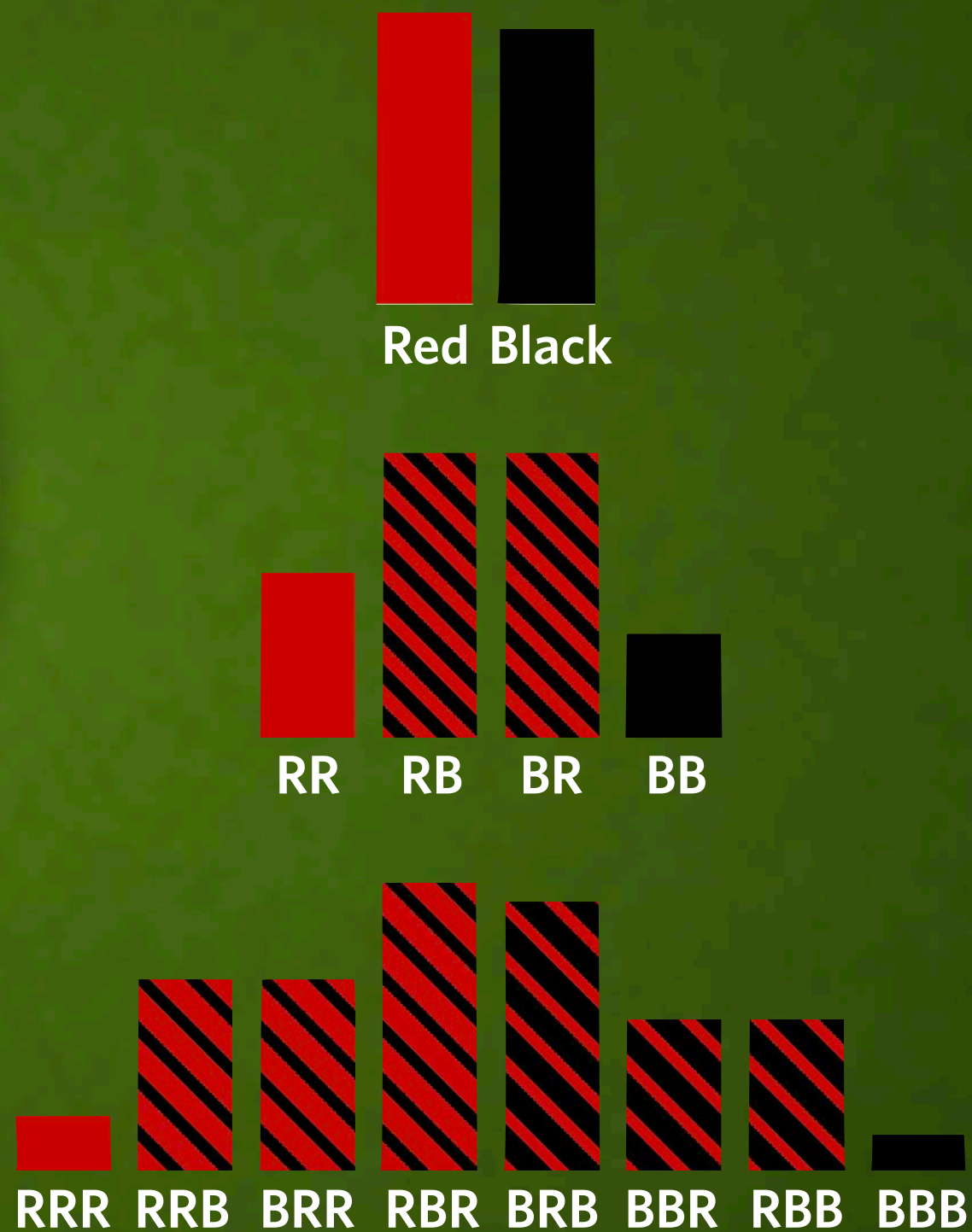
Monopoly



Roulette



Roulette

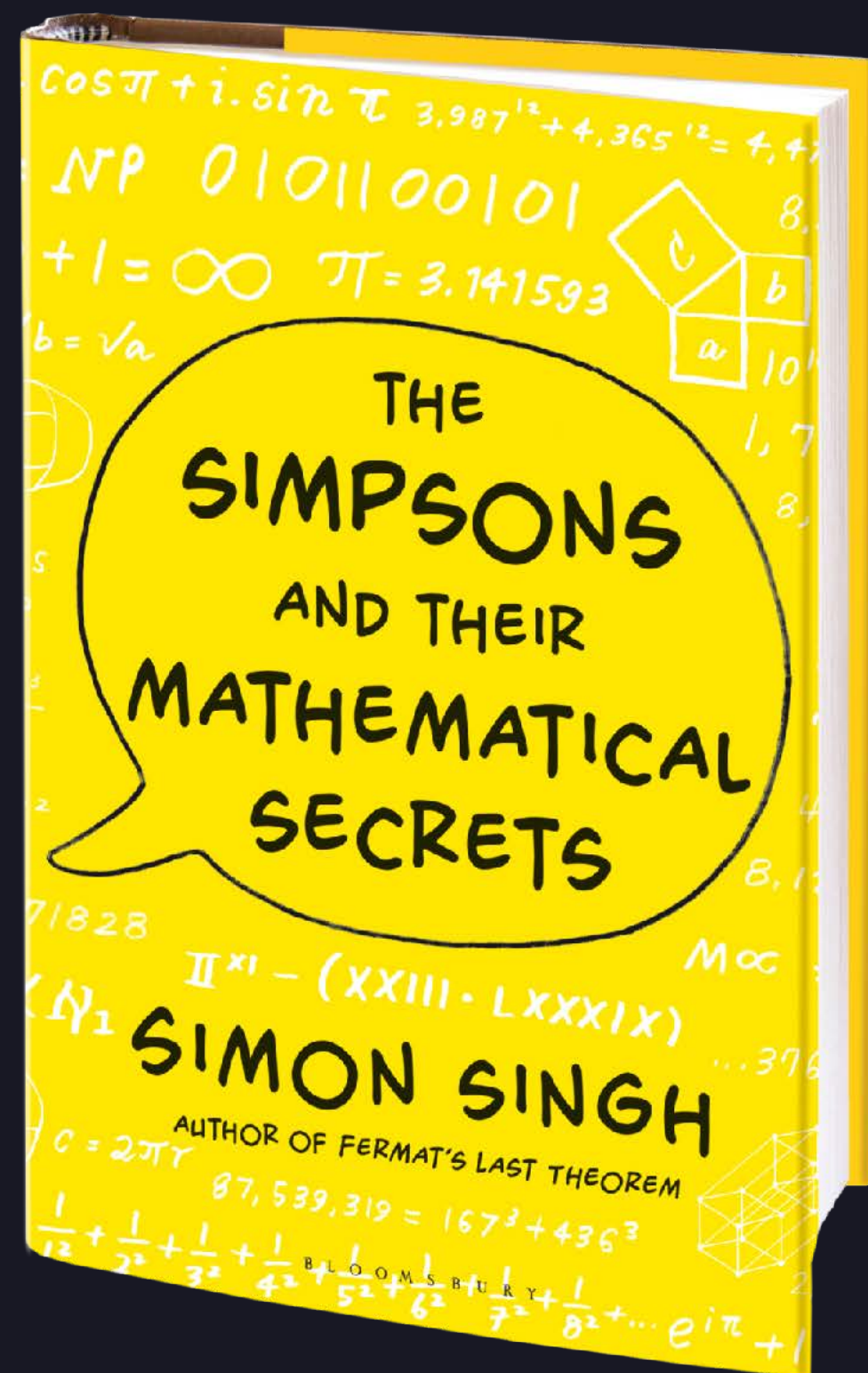


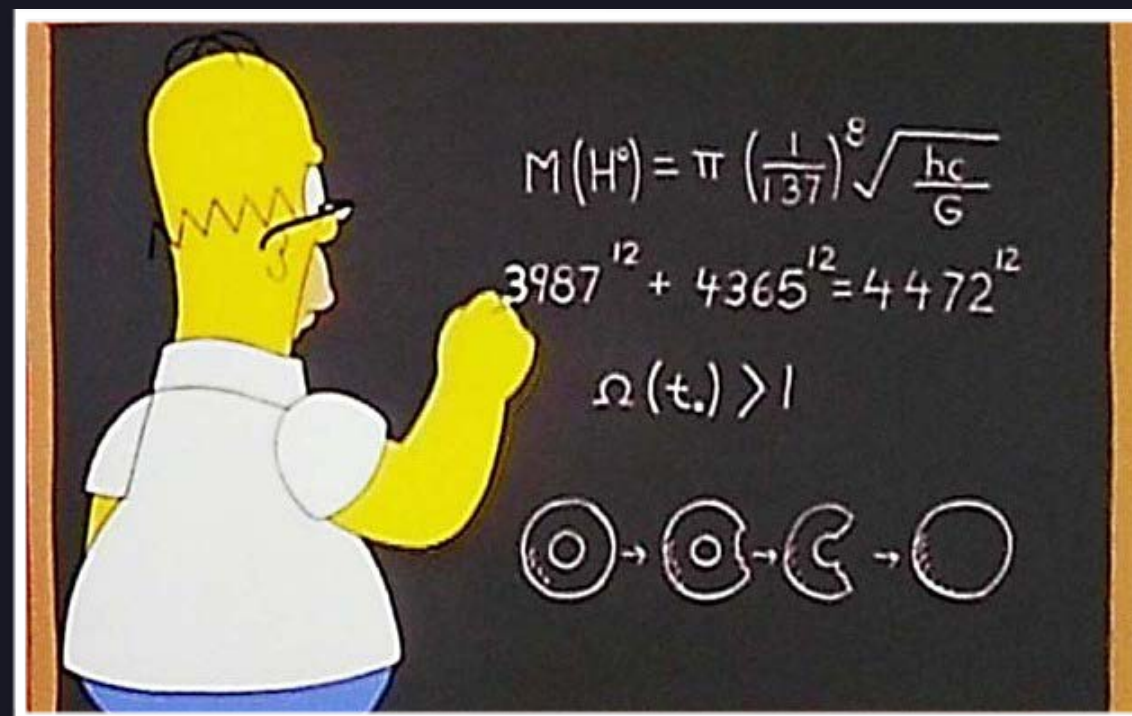
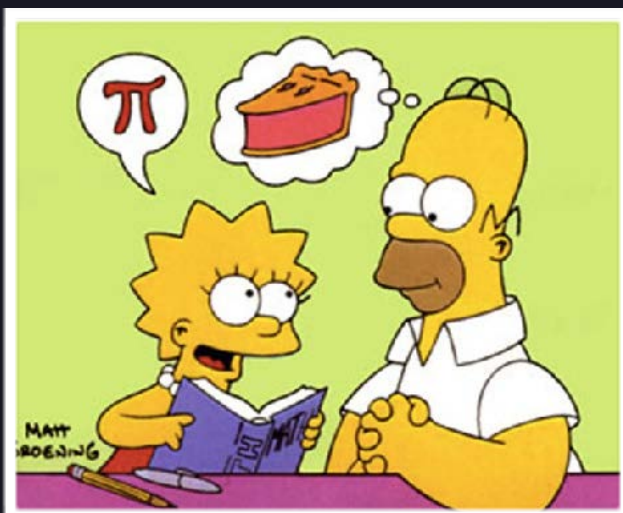
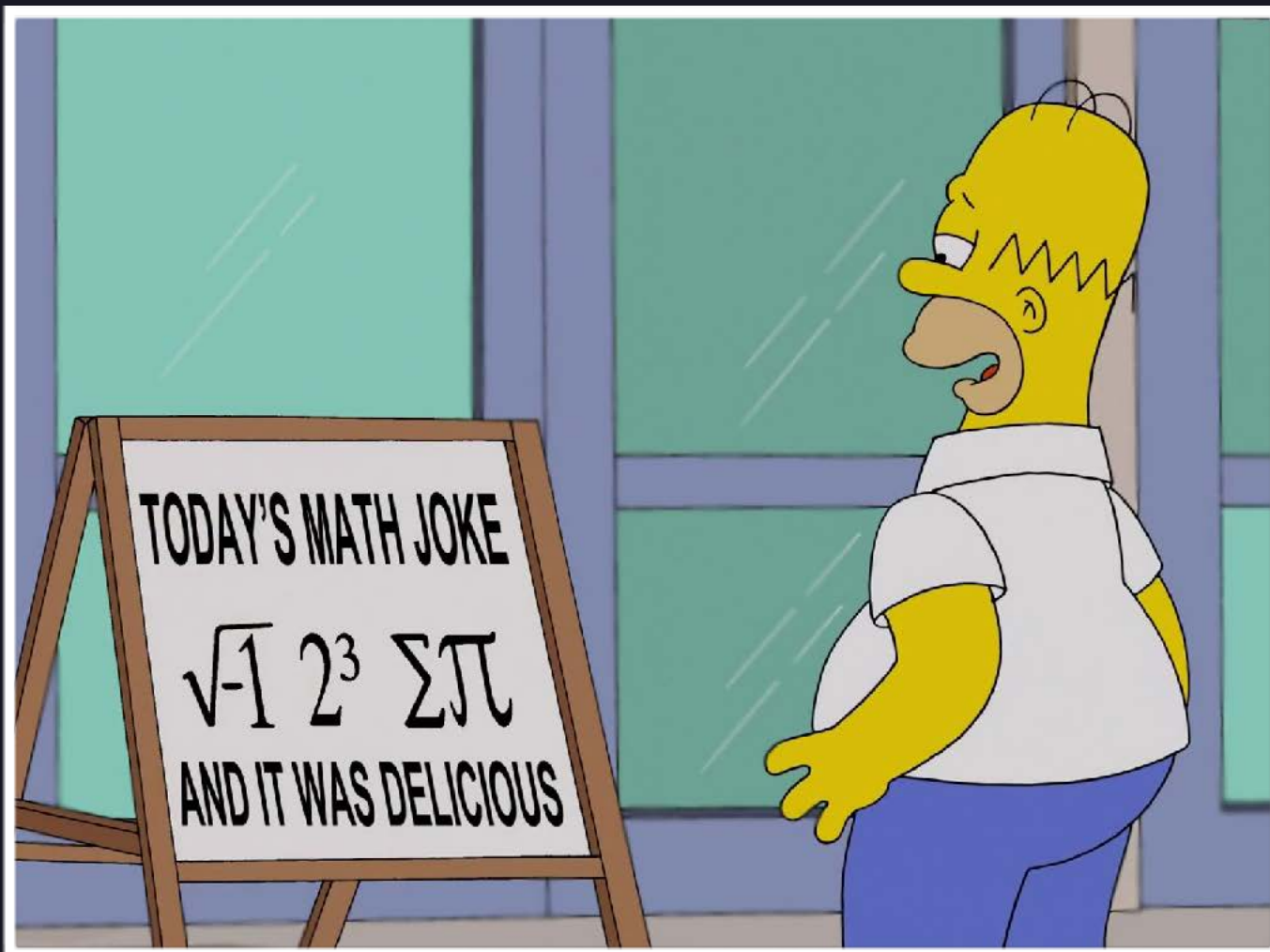


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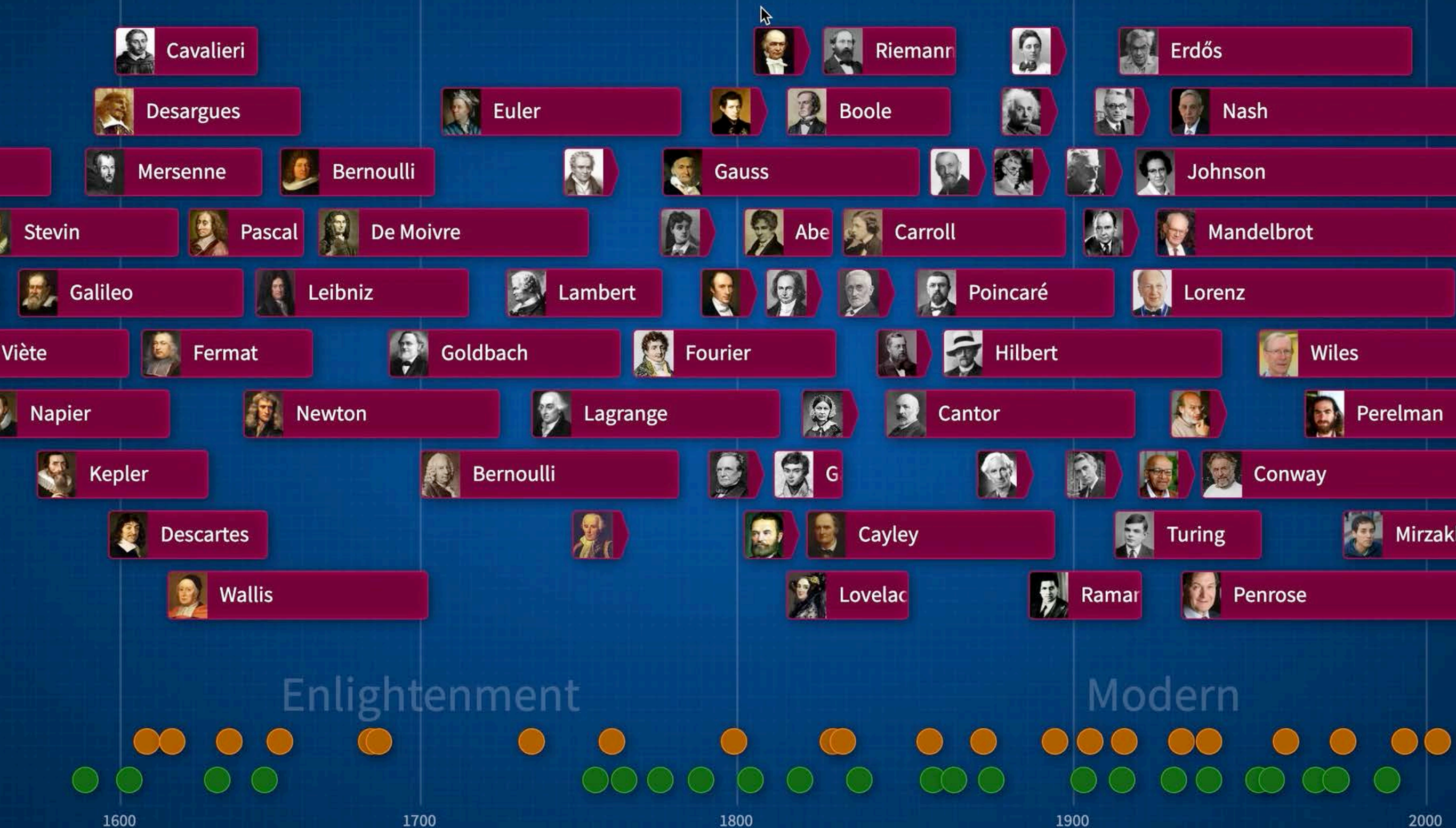


Lottery





Timeline of Mathematics





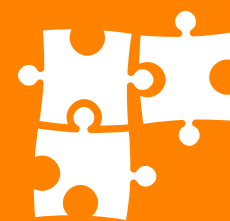
Mathematics is filled with Stories!



Applications



**Science
and Nature**



**Games and
Puzzles**



**History and
Mathematicians**



Fiction



Stories are great for teaching!

**Get students
excited and
motivated**

**Make the
content more
memorable**

**Show careers
and people
who use math**

**Encourage to
keep studying
math and STEM**



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Creativity

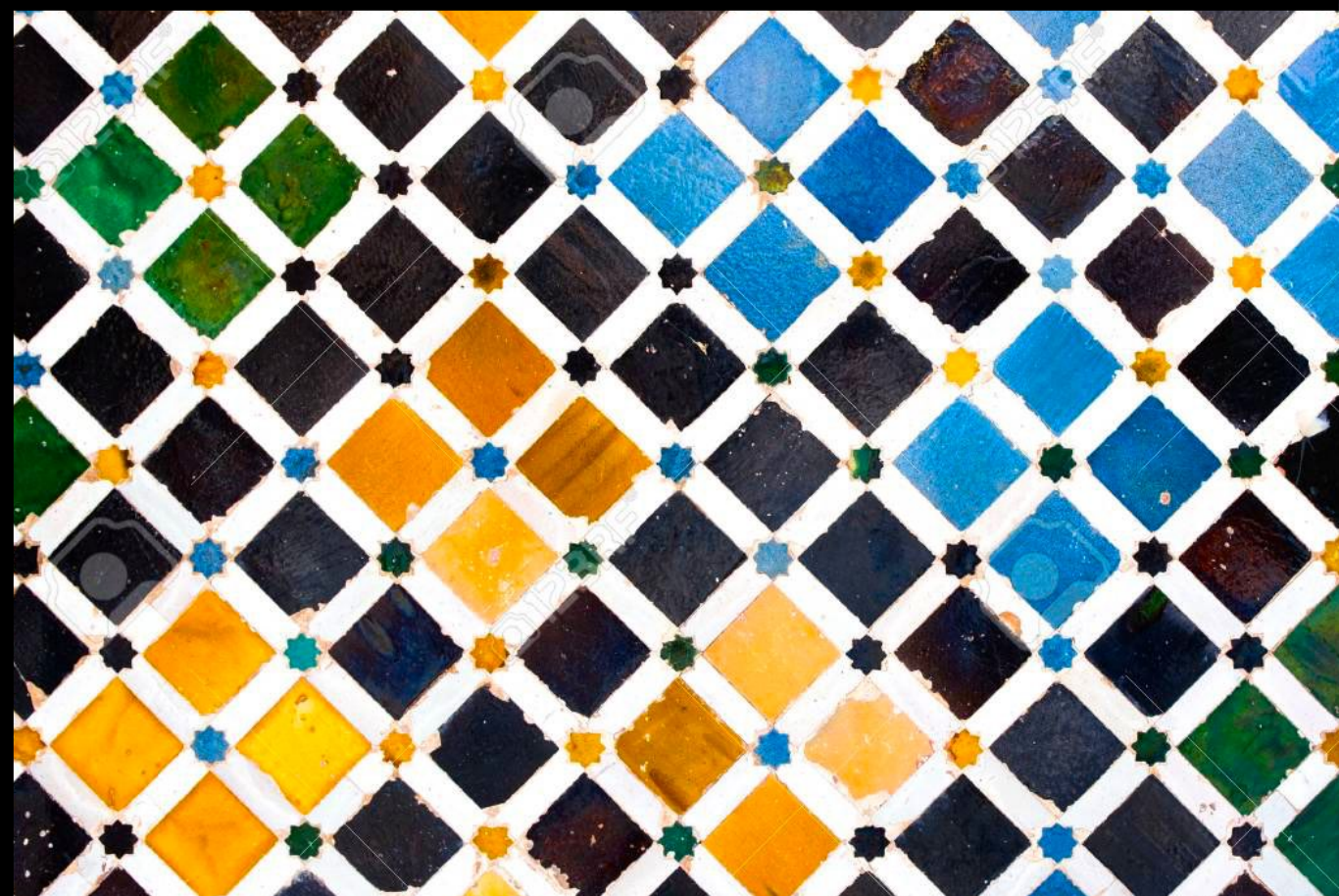
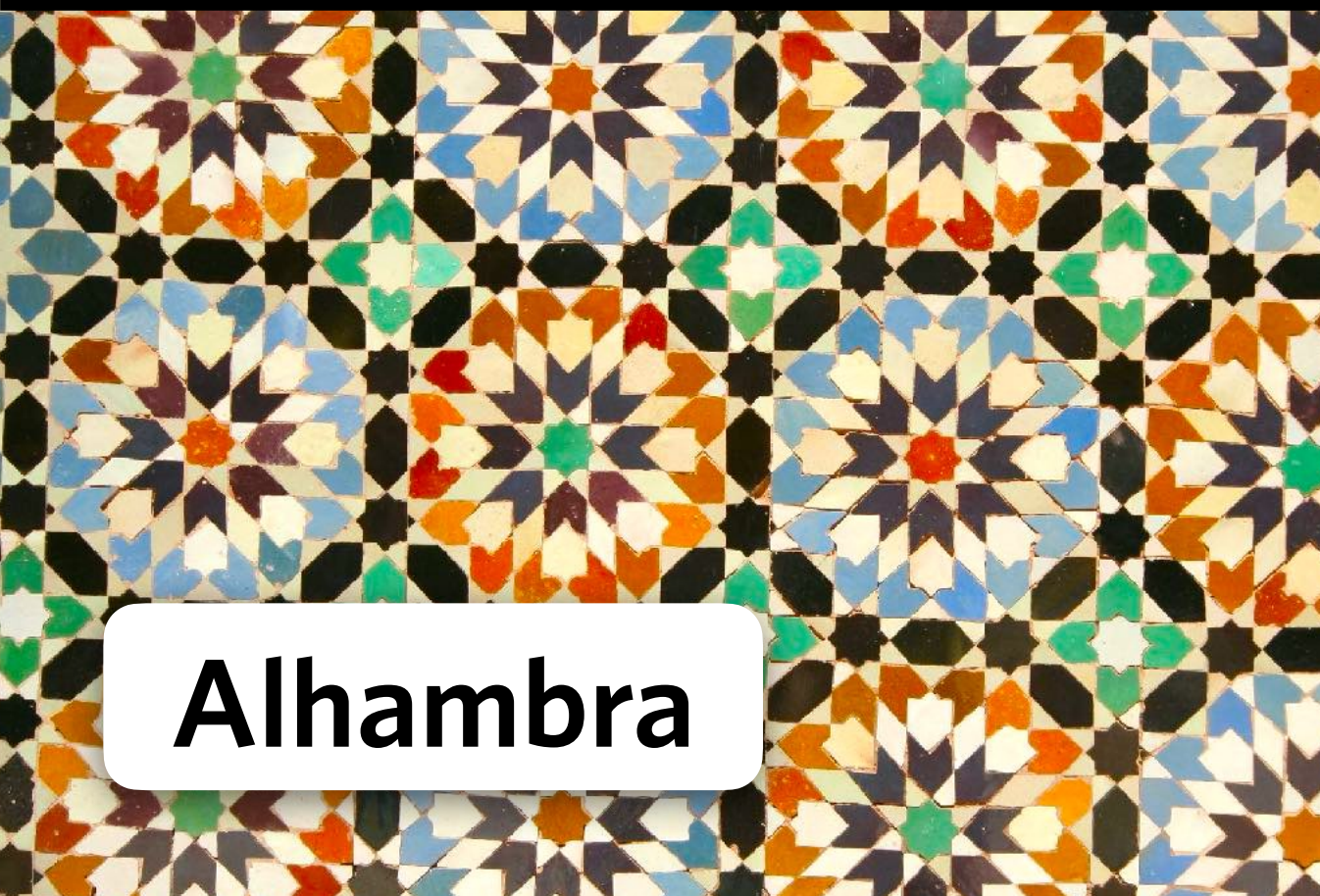
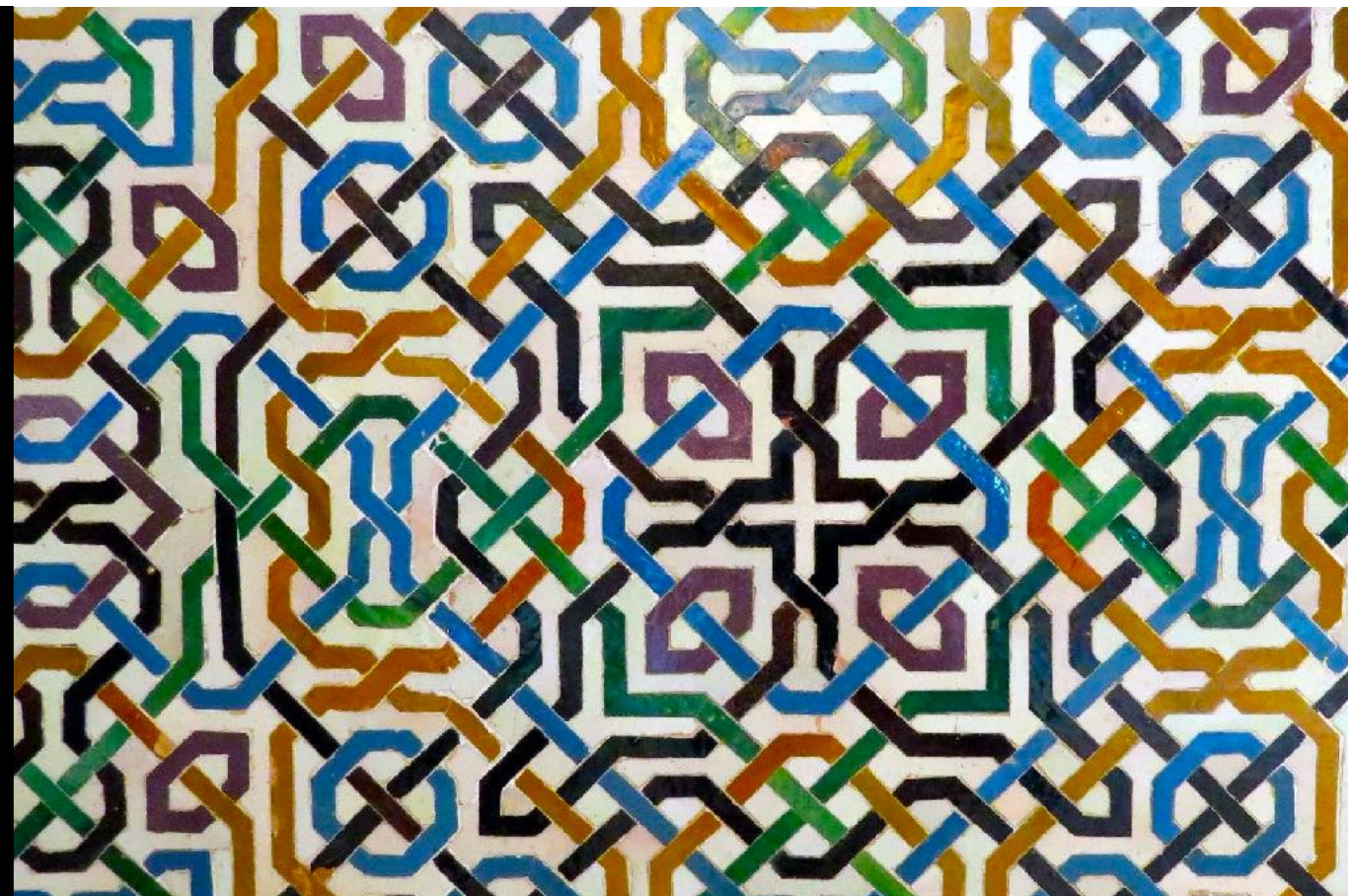


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Tessellations



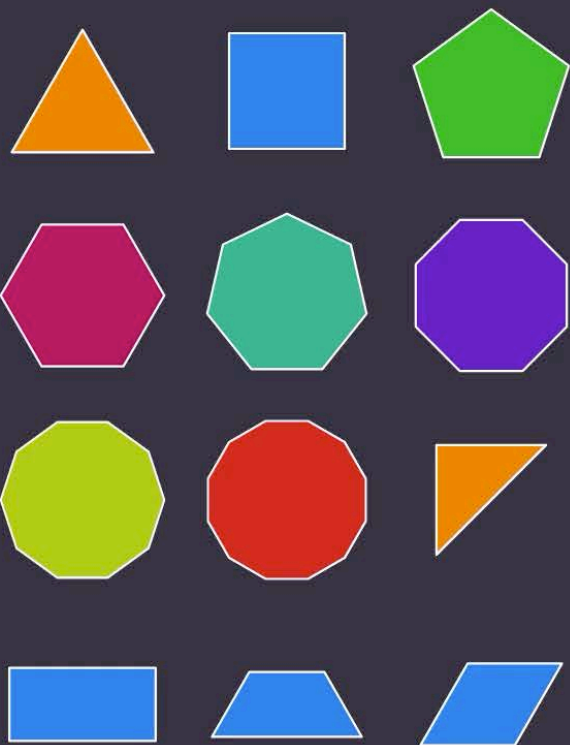
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Alhambra



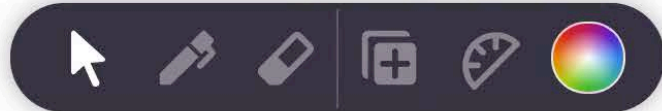
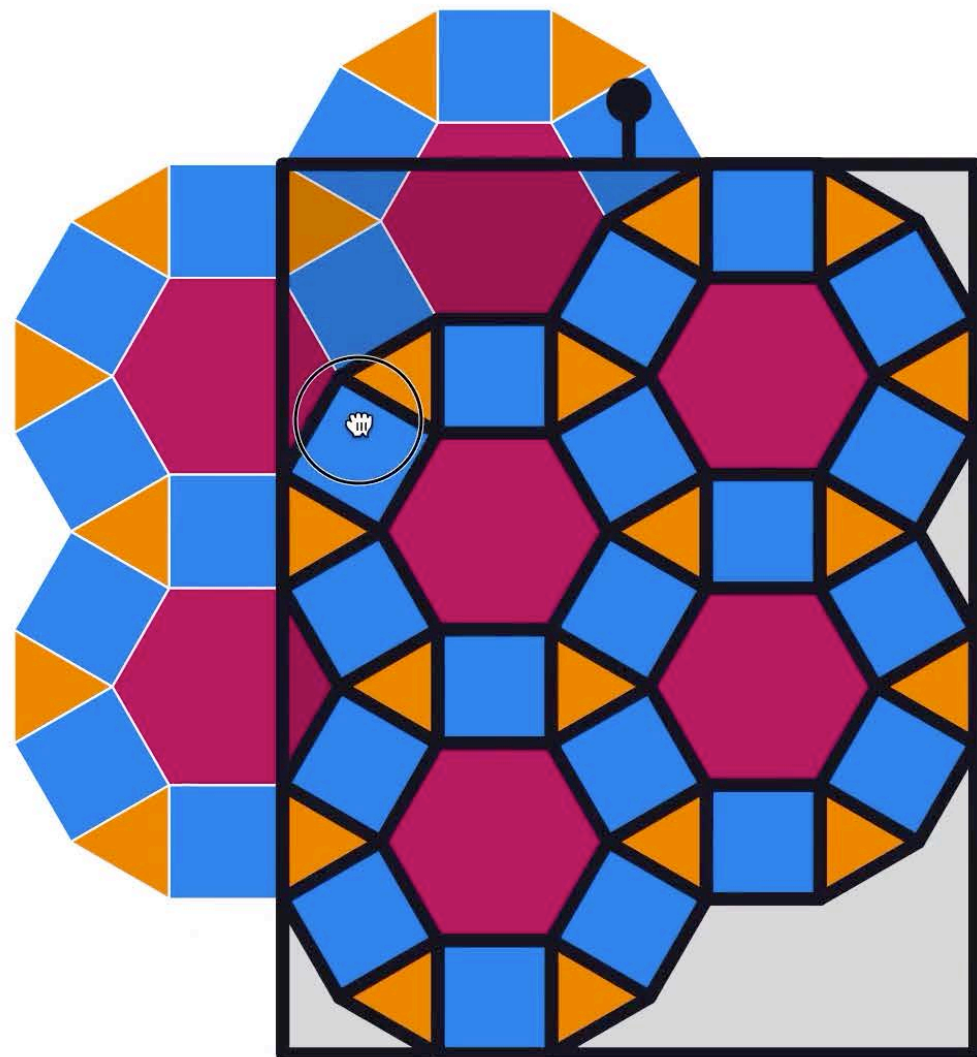
POLYGONS

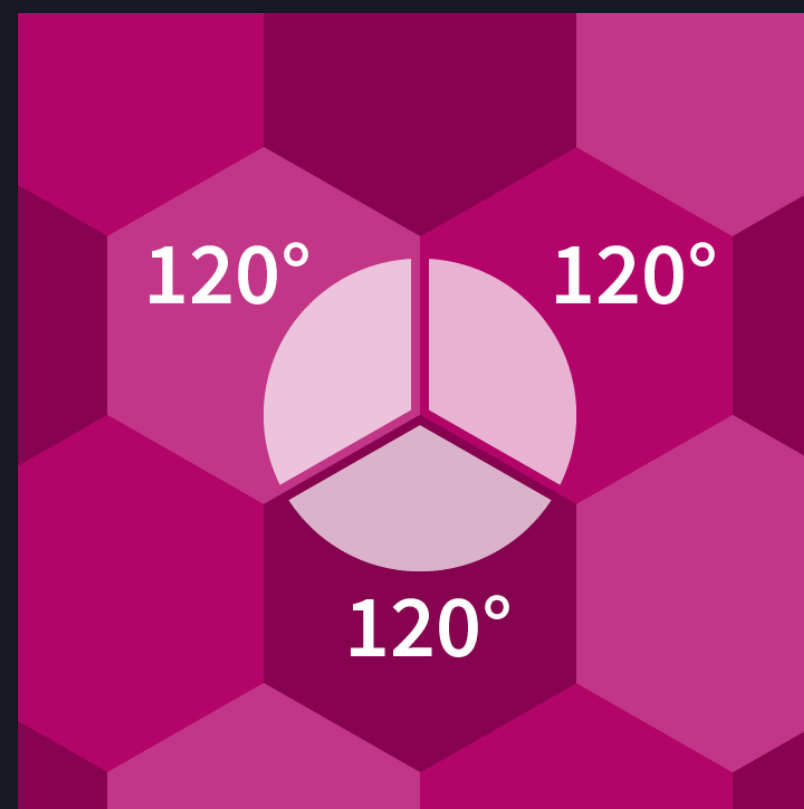
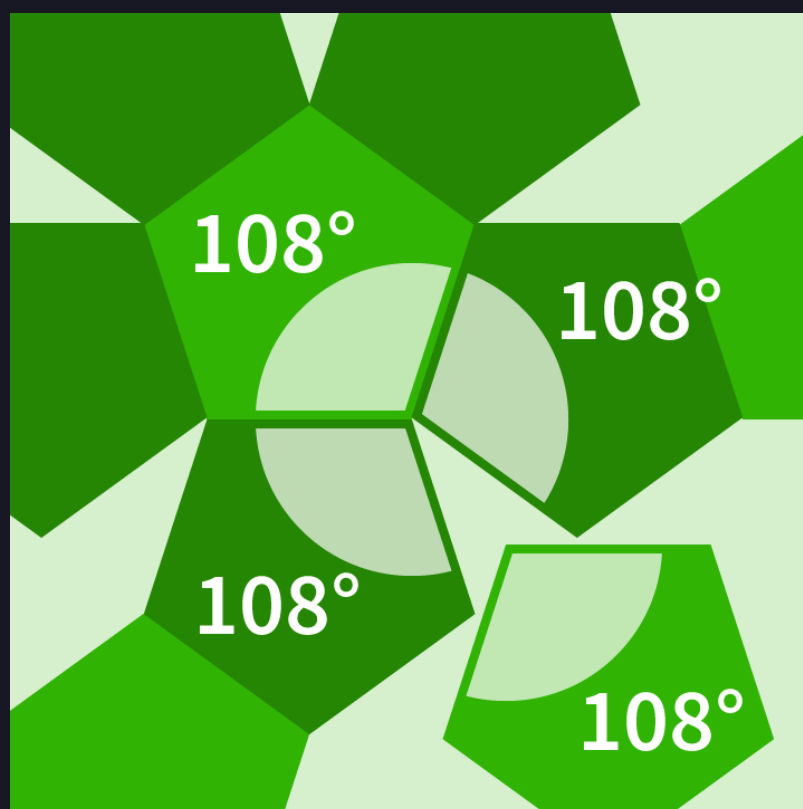
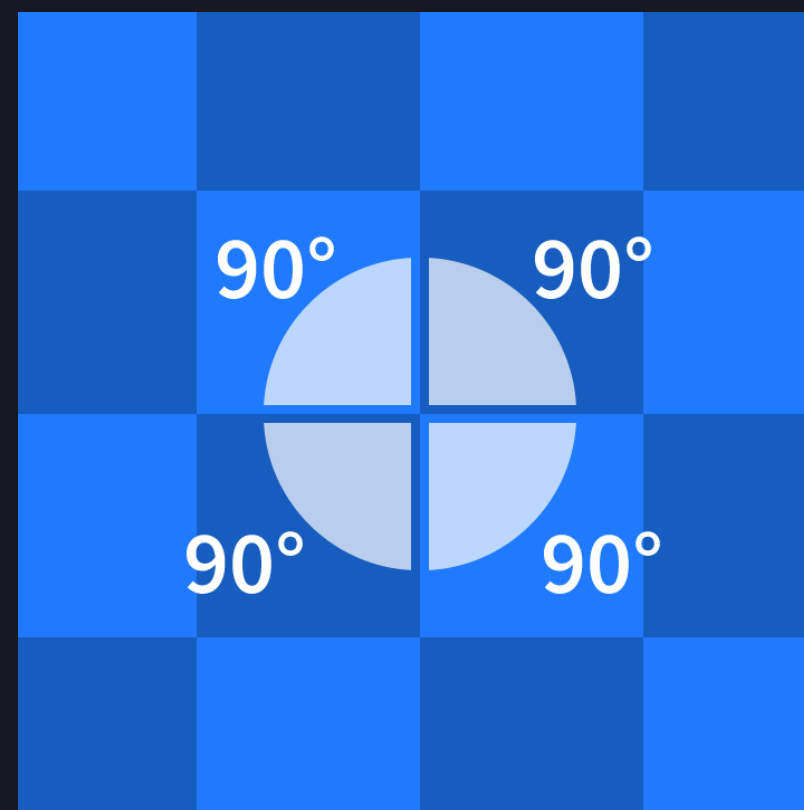
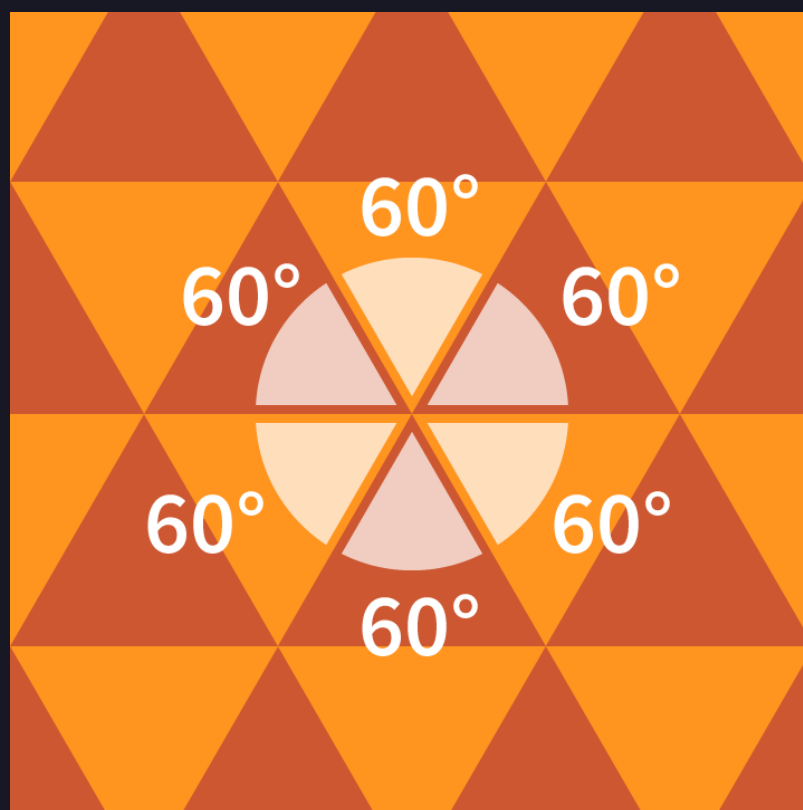


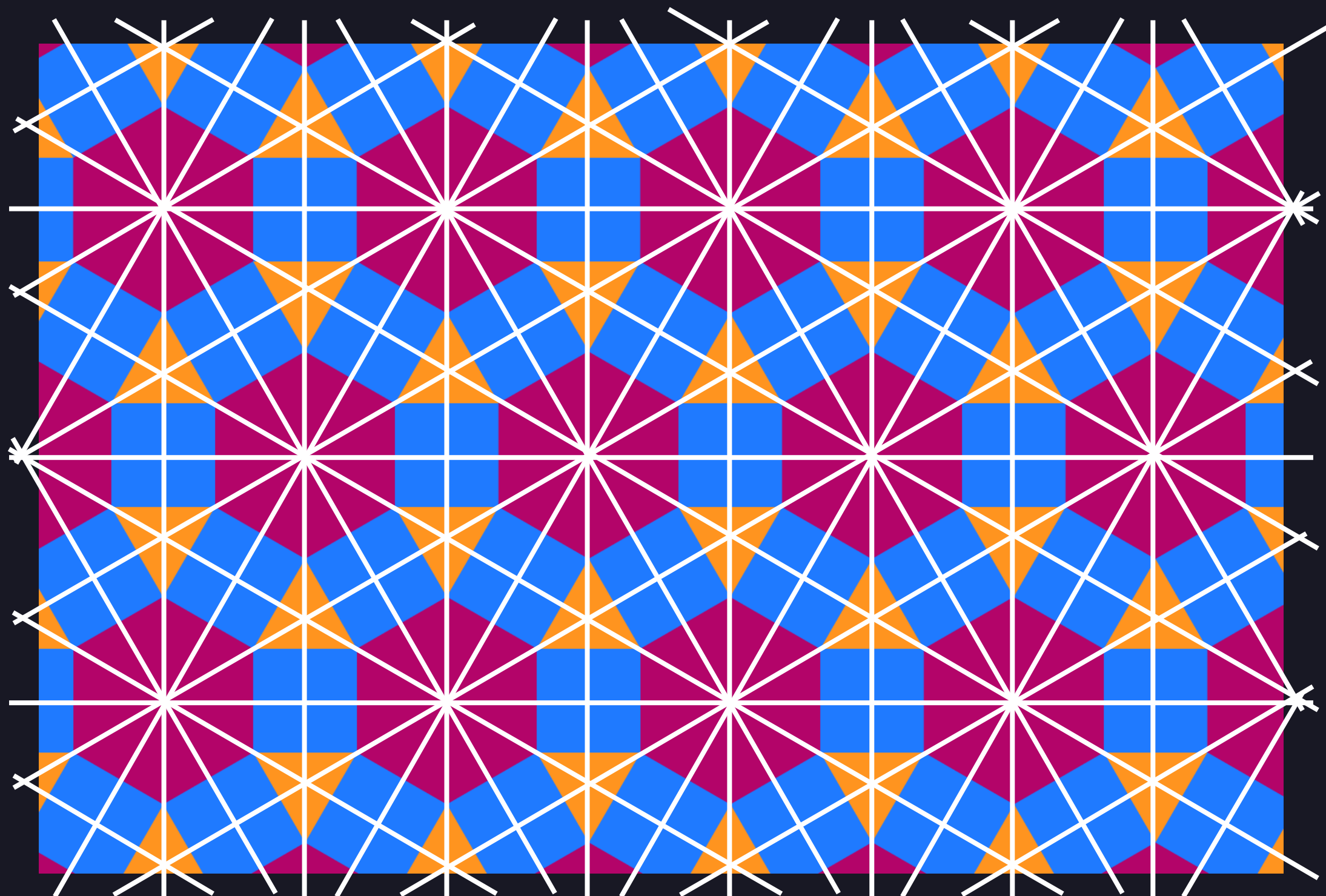
NUMBER TILES



NUMBER BARS

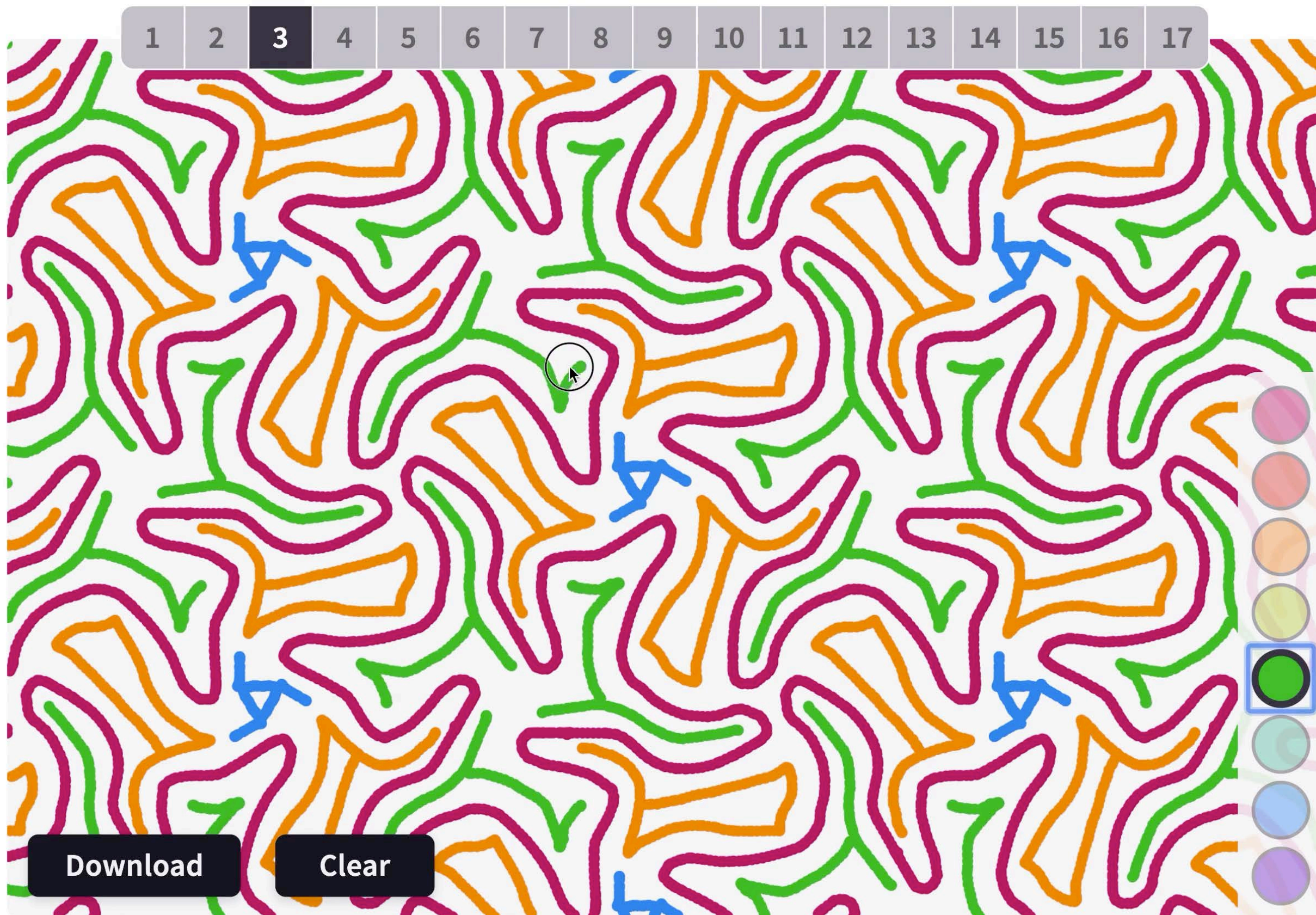


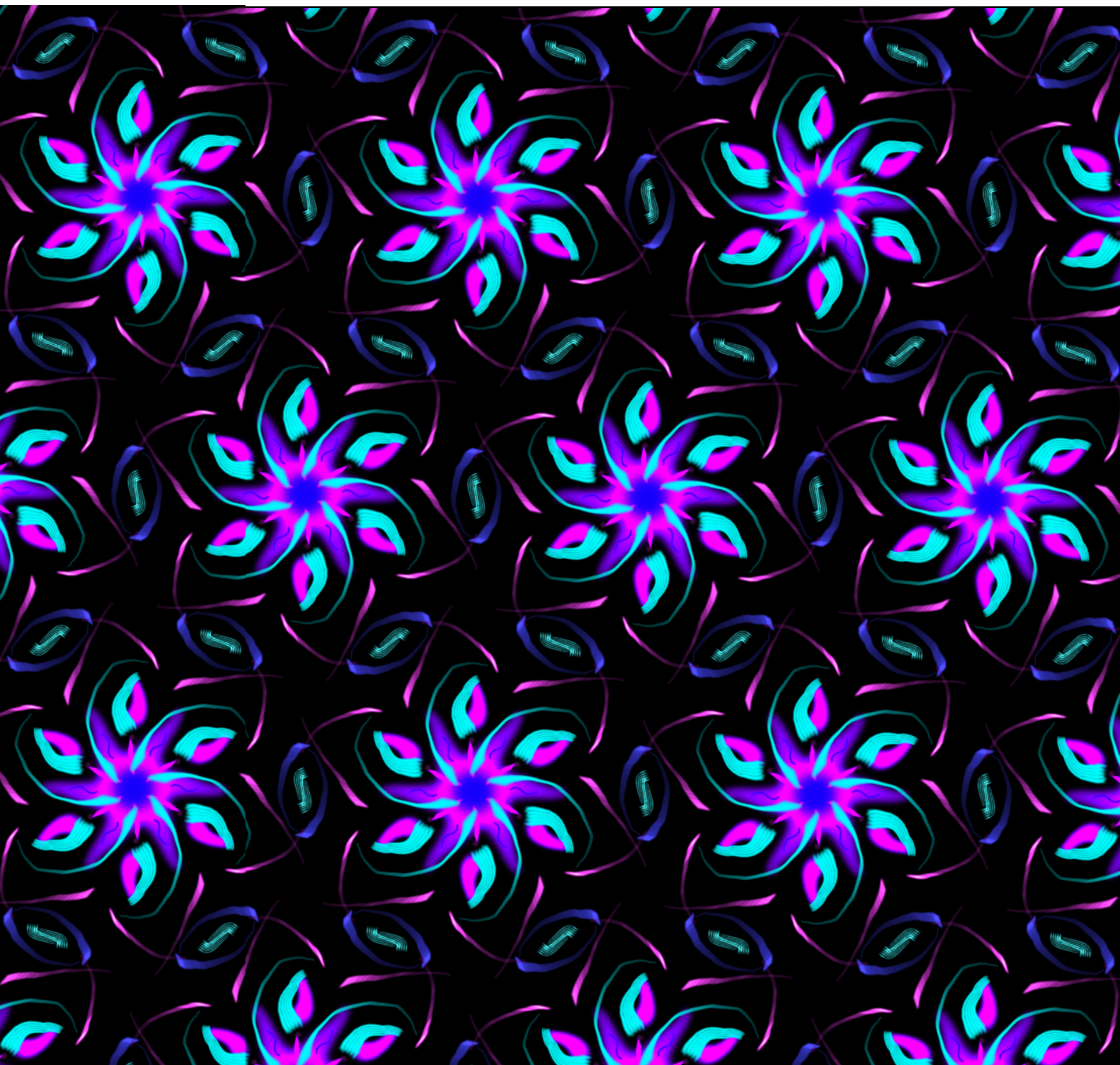






17 Wallpaper Groups

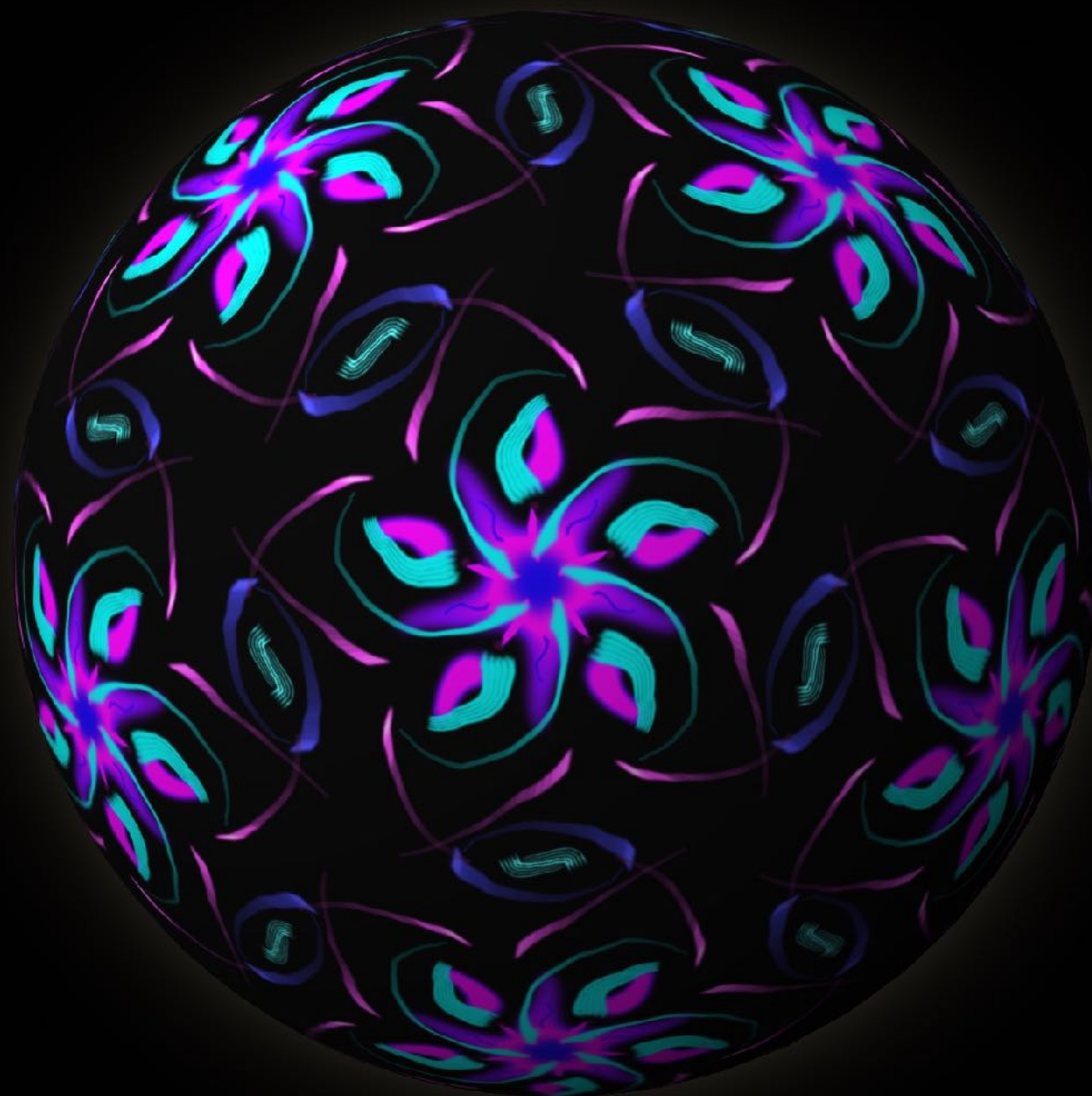
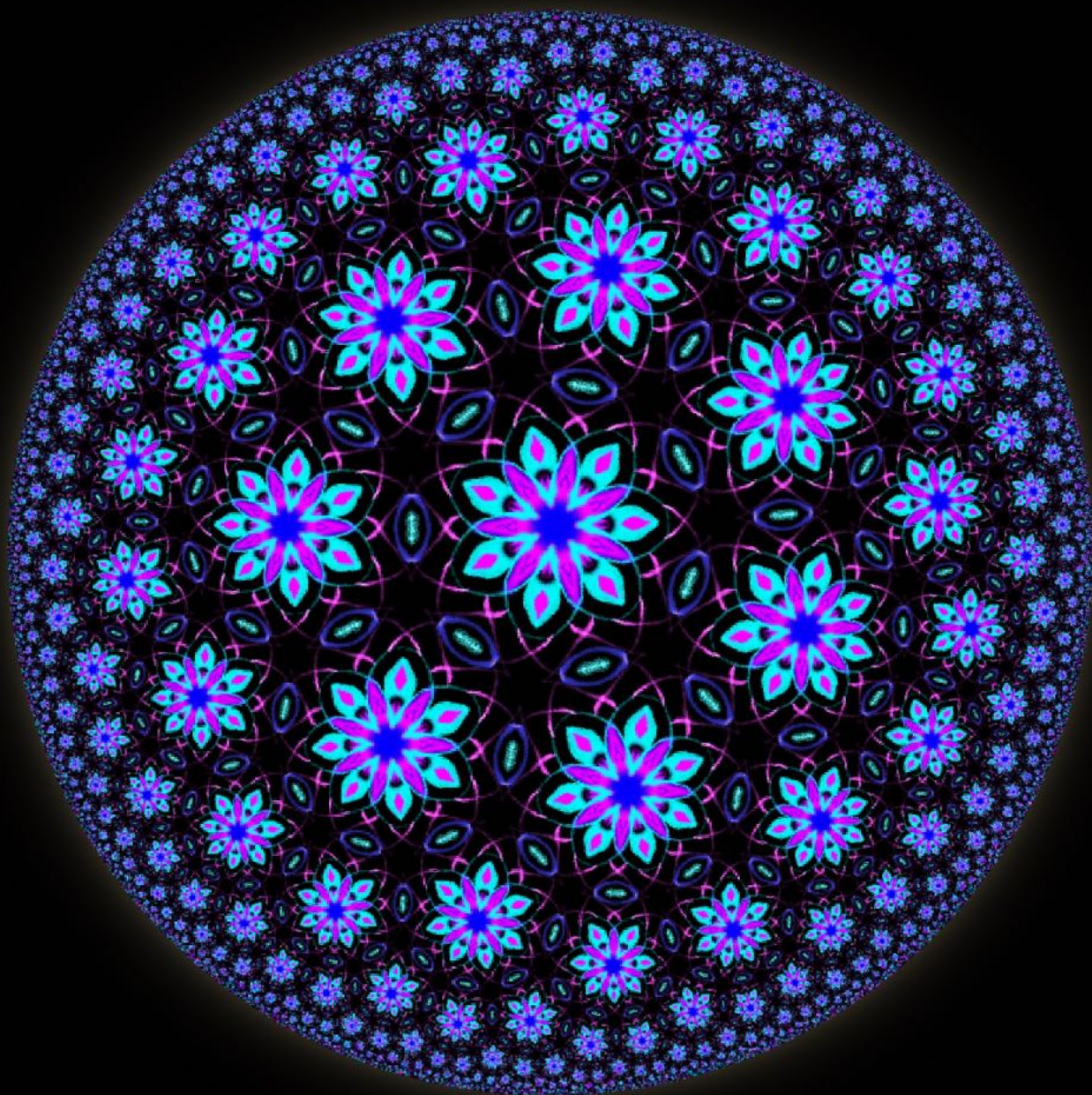


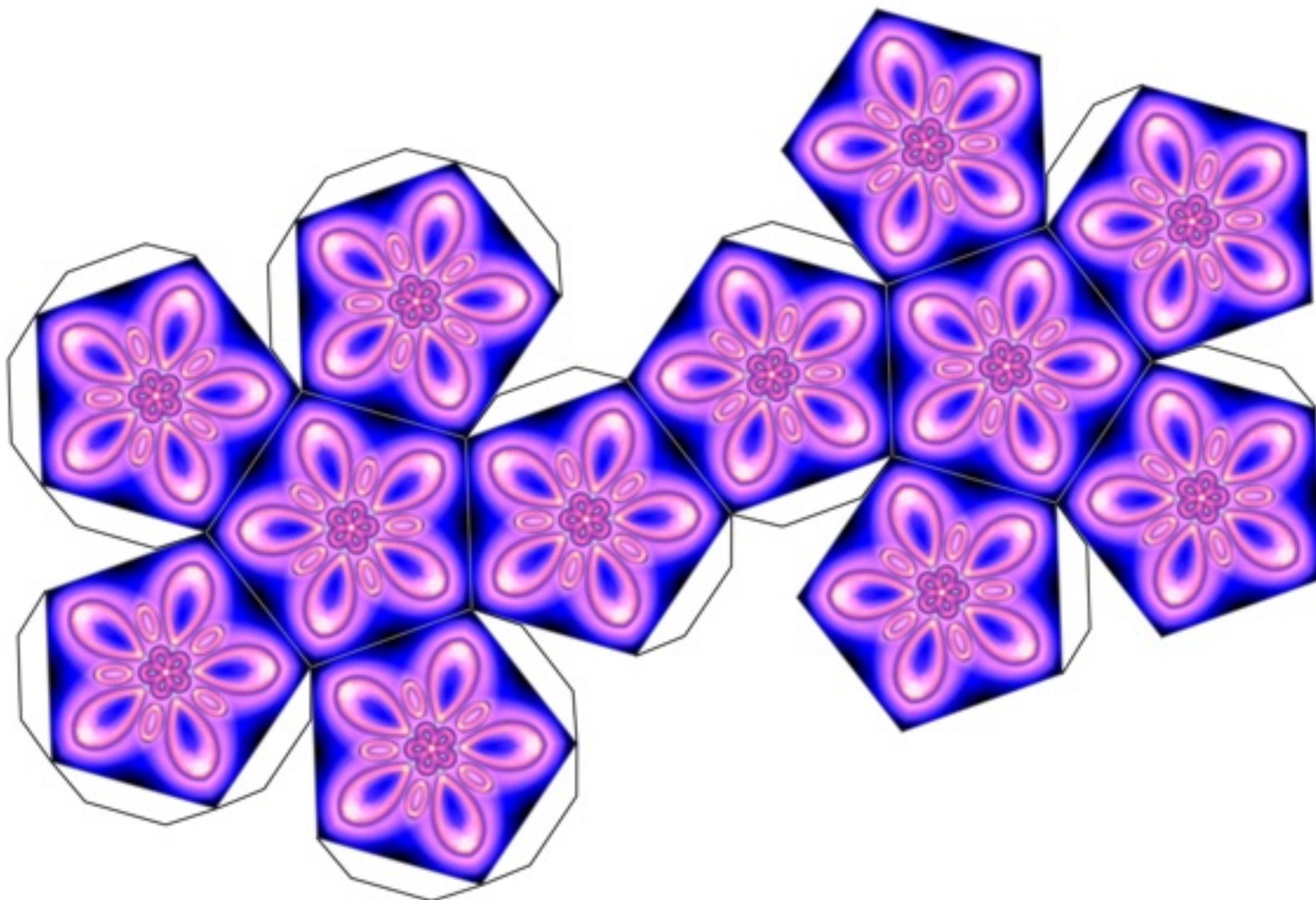




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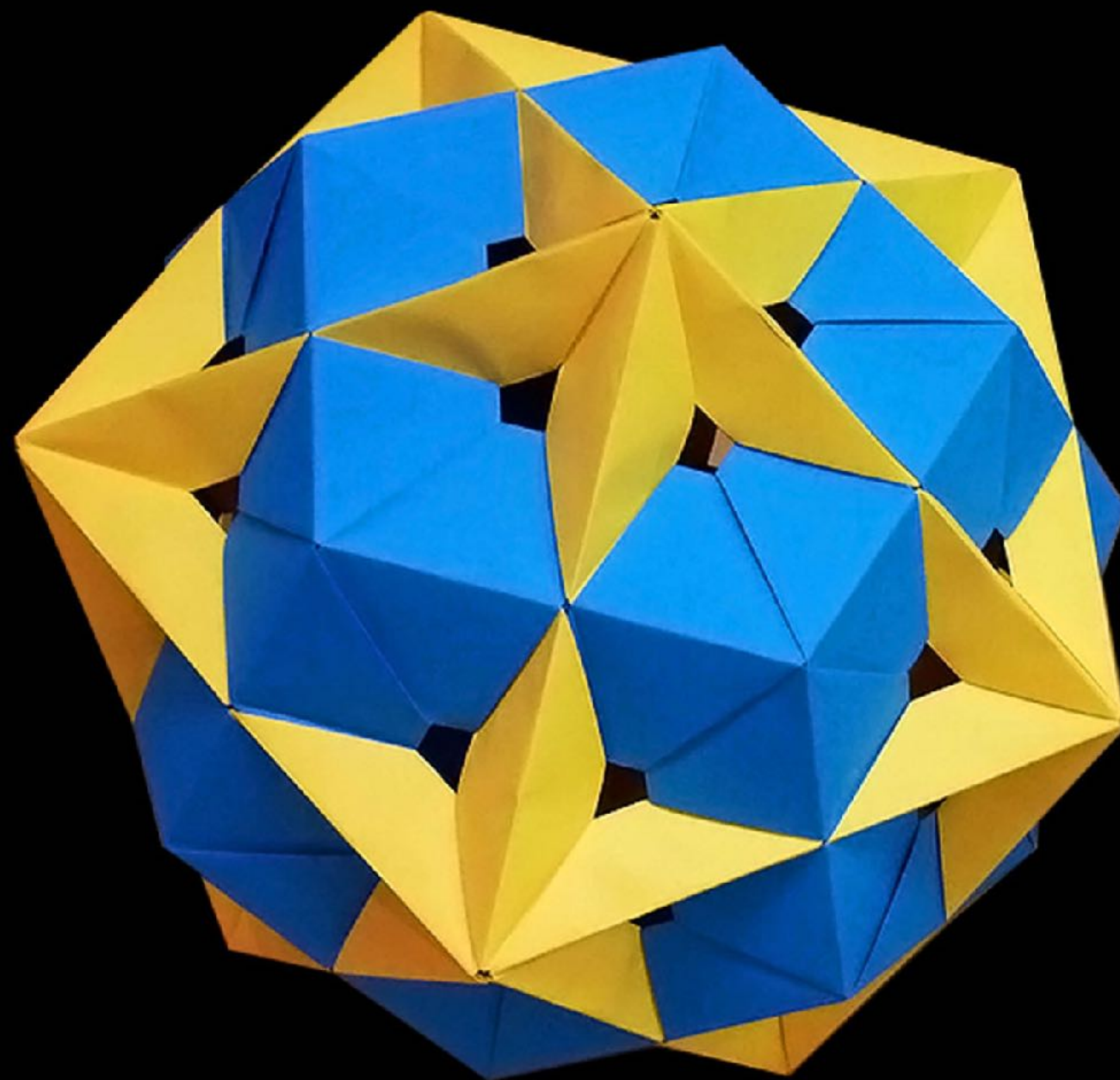
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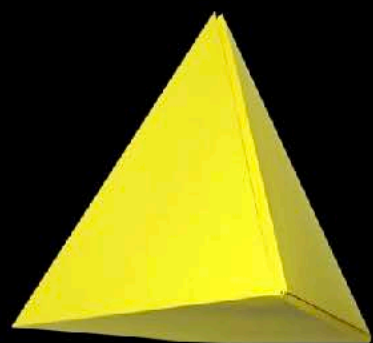
Polyhedra



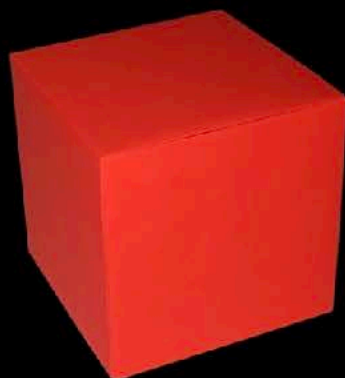


Volume
Surface Area
Nets/Cross Sections
Euler's Formula
5 Platonic Solids





Tetrahedron



Cube



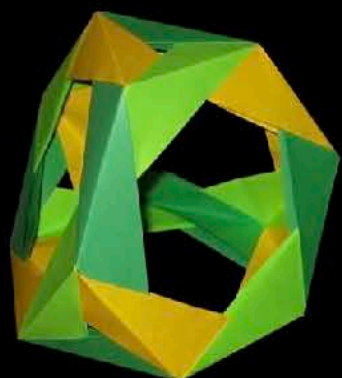
Octahedron



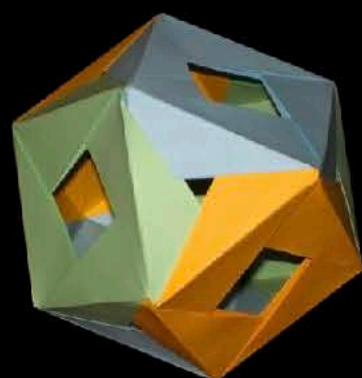
Dodecahedron



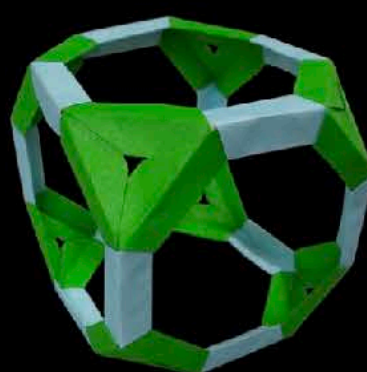
Icosahedron



Truncated Tetrahedron



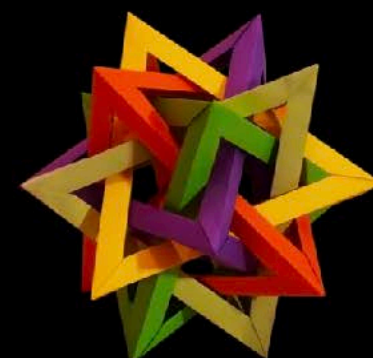
Cuboctahedron



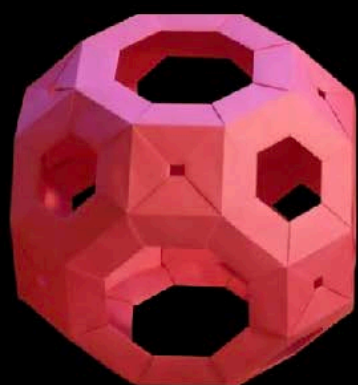
Truncated Hexahedron



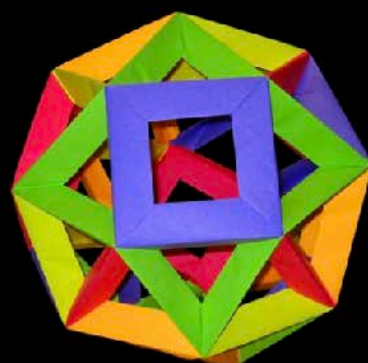
Truncated Octahedron



Intersecting Tetrahedra



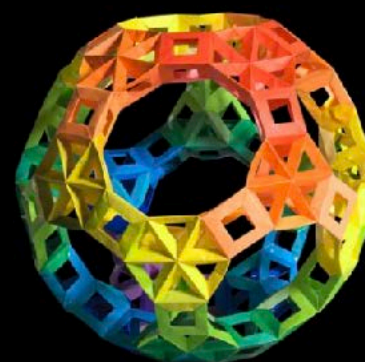
Truncated Cuboctahedron



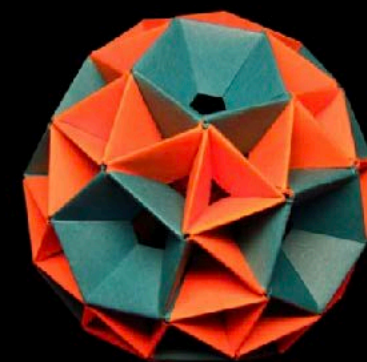
Snub Cube



Icosidodecahedron



Truncated Icosidodecahedron



Snub Dodecahedron

MATHIGON ORIGAMI
DRAGONS ★ ★ ★

more on mathigon.org/origami/

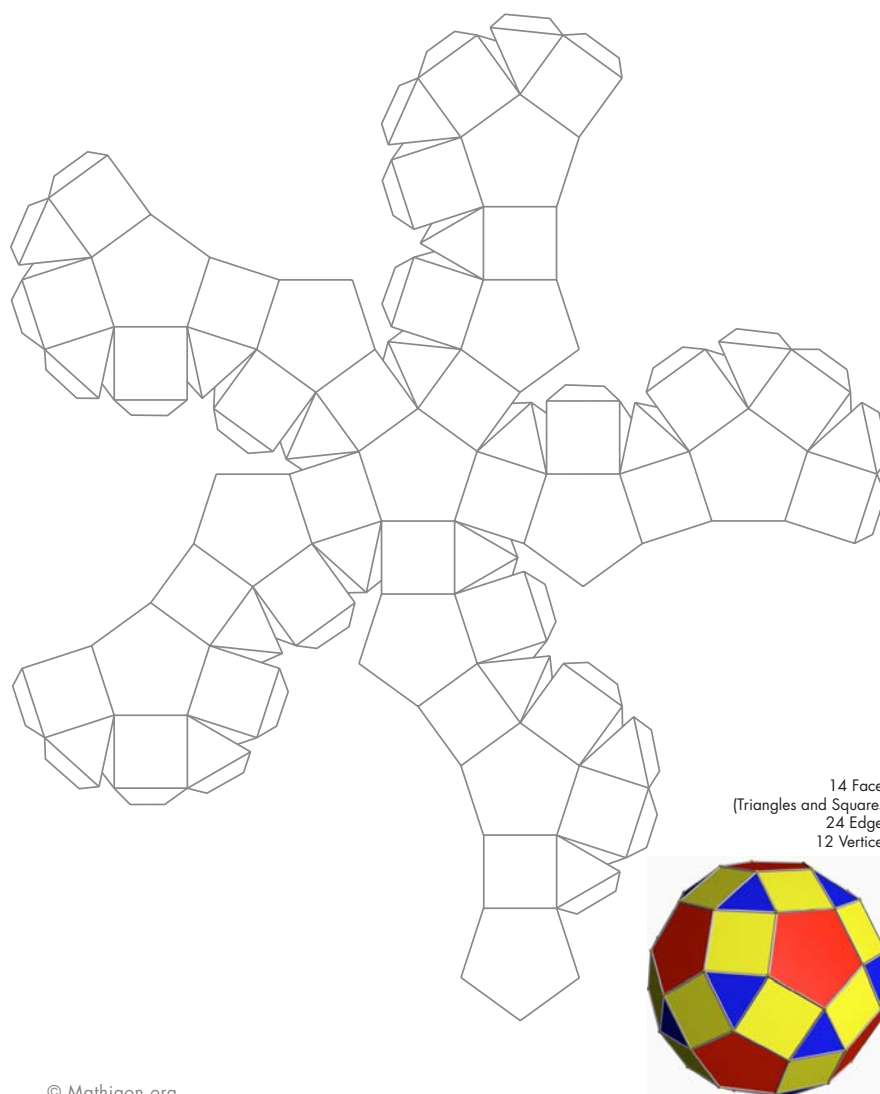
This model requires one quadratic sheet of paper.

Crease horizontally and vertically along centre.	Flip over and fold along both diagonals.	Put two opposite corners on top of each other, to create a smaller square.	Fold the bottom edges towards the centre.
Repeat previous step on opposite side.	Fold top triangle down.	Unfold the previous three steps.	Fold the bottom corner upwards.
Repeat previous step on opposite side.	Fold top two edges towards the centre.	Repeat previous step on opposite side.	'Close' the front two sides and repeat on the back.
Rotate by 180° and fold the first wing.	Fold top edges towards centre as shown.	Repeat previous two steps to create the second wing.	Fold up the neck of the dragon.
Fold neck twice in opposite directions for the head.	Fold the tail upwards.	Add additional creases to both wings.	This is the final Origami Dragon.

© Mathigon.org

MATHIGON ORIGAMI
RHOMBICOSIDODECAHEDRON

more on mathigon.org/origami/



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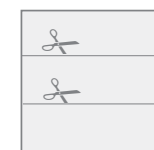
MATHIGON ORIGAMI
5 INTERLOCKING TETRAHEDRA ★ ★ ★ ★

more on mathigon.org/origami/

This model consists of the interlocking frames of five tetrahedra. It is one of the most difficult models on Mathigon.org, but also the most impressive.

Every tetrahedron is made out of six strips of paper with dimensions in the ratio 1:3. These can be created by cutting a square into three parts. We recommend that you use different colours for every tetrahedron, which means you need two squares in each of five colours.

Once you have created all $5 \times 6 = 30$ strips, they each need to be folded as follows:



Fold along centre, then unfold.	Fold both edges towards centre, don't open.	Fold both edges towards centre again, unfold.	Fold bottom corner onto line in centre of top half.
Repeat for top corner.	Unfold.	Fold bottom corner inwards.	Fold top corner as shown.
Rotate unit and repeat steps 3 to 8 at opposite end.	Fold entire unit along its centre.		

Each of these 30 units will form the edge of one tetrahedron. At every vertex, three units link together:

--	--	--	--

Now start connecting all units colour by colour, to form the five interlocking tetrahedra.

Connect all 6 units in any one colour to make the first tetrahedron.	For the second and third tetrahedra, first create one corner ('tripod') and interlink it with the existing shape. Then lock it in place using the remaining three edges of that colour.	Add the fourth and fifth Tetrahedra in a similar way.

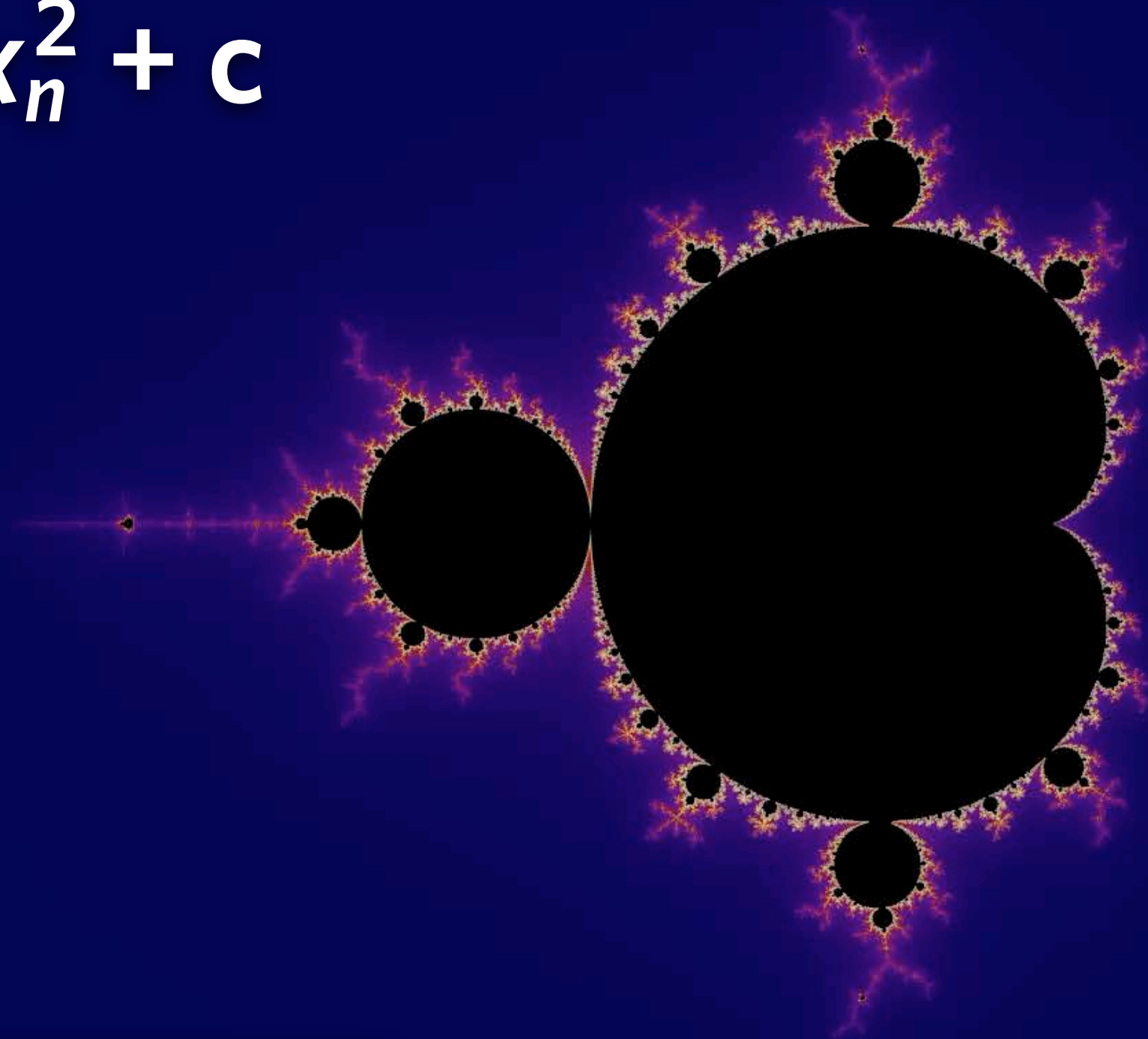
© Mathigon.org



Intersecting Tetrahedra



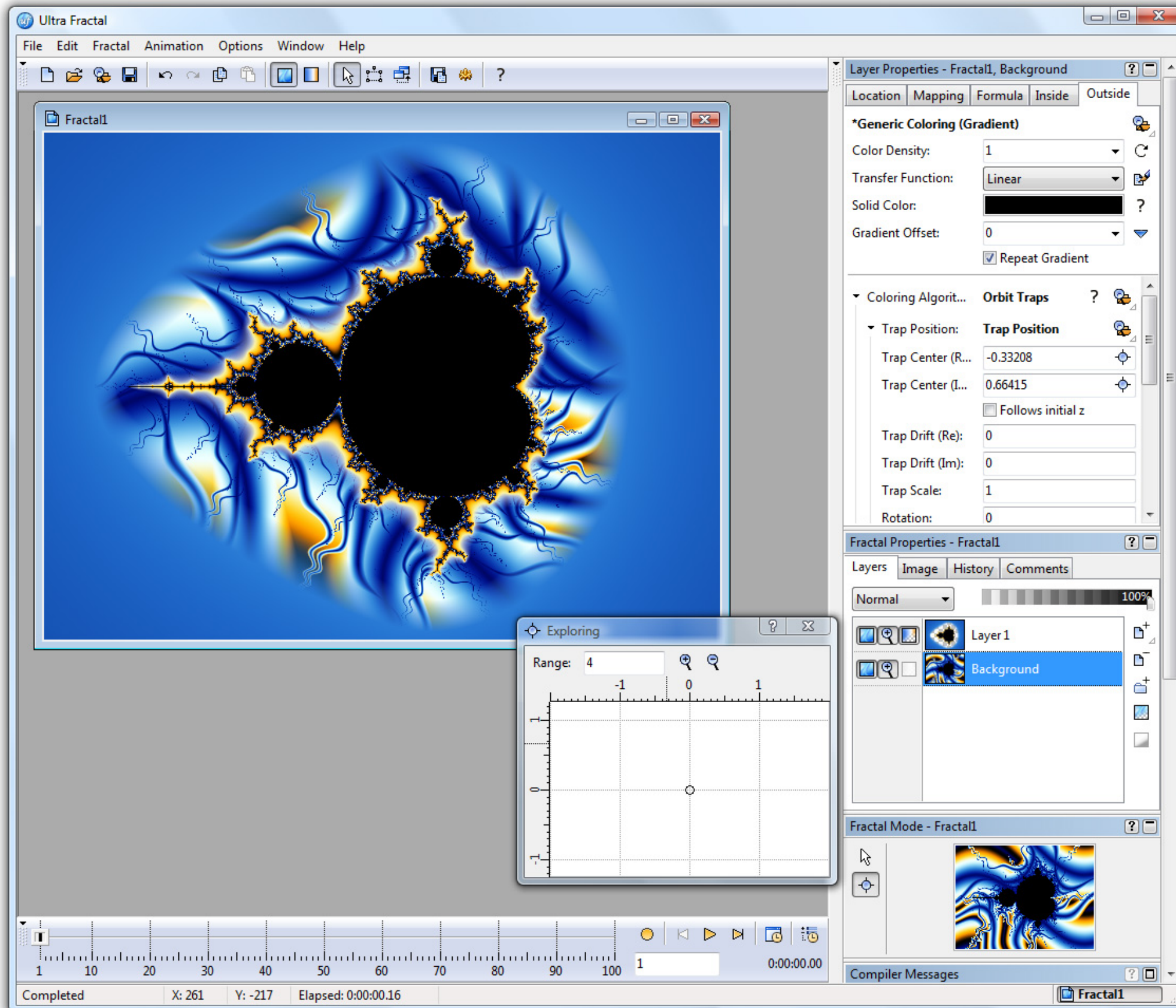
$$x_{n+1} = x_n^2 + c$$

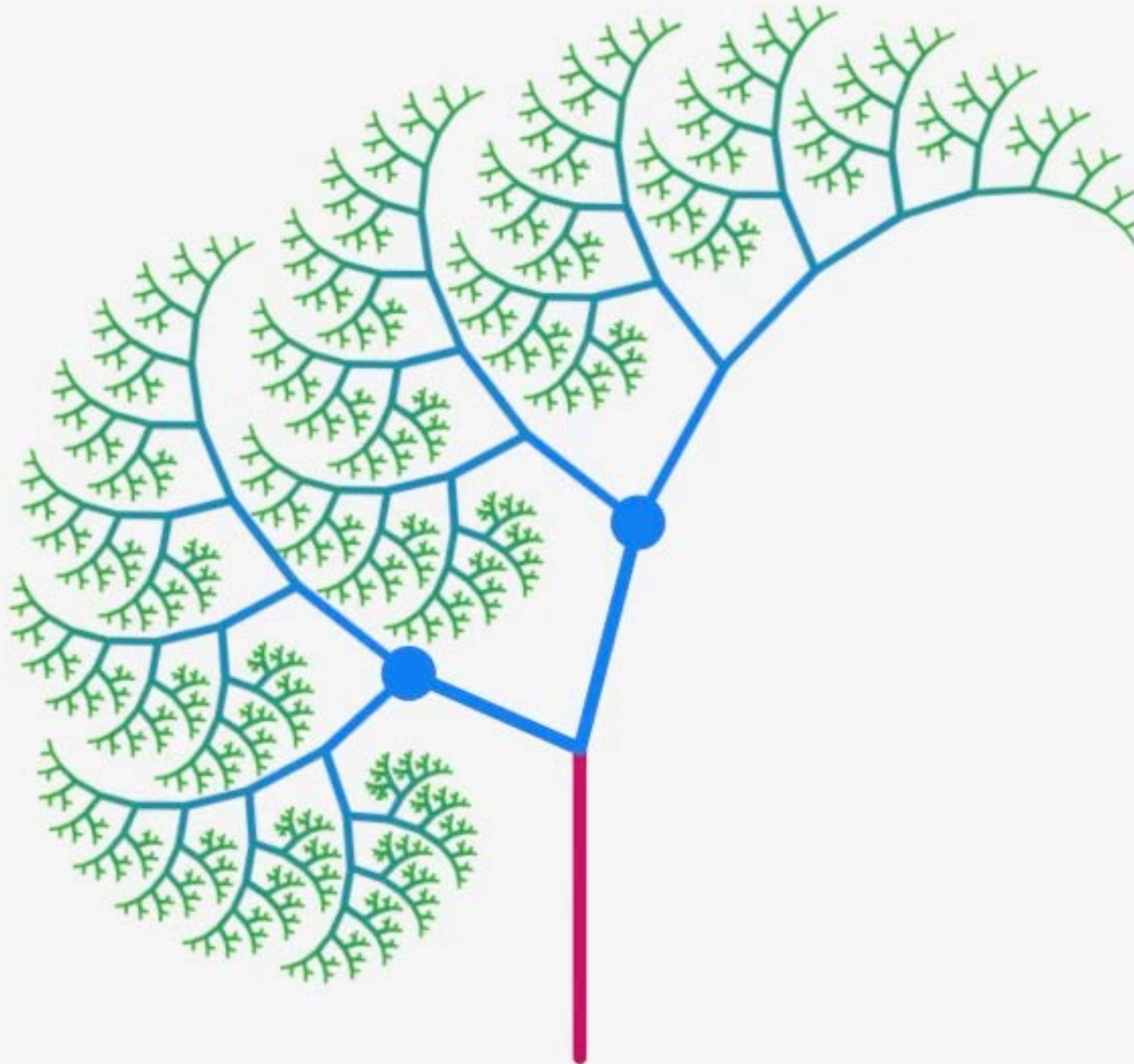


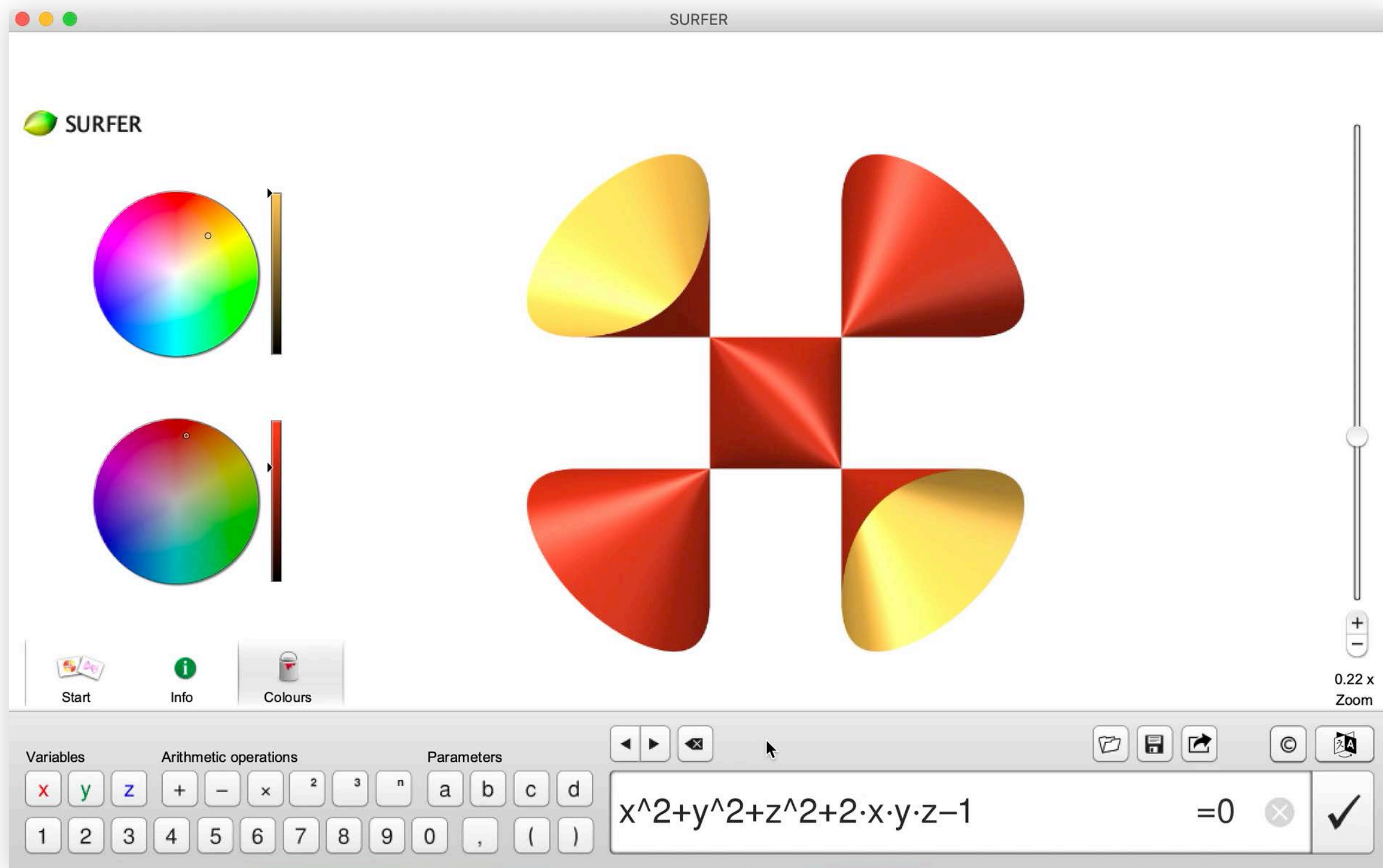
Mandelbrot Set

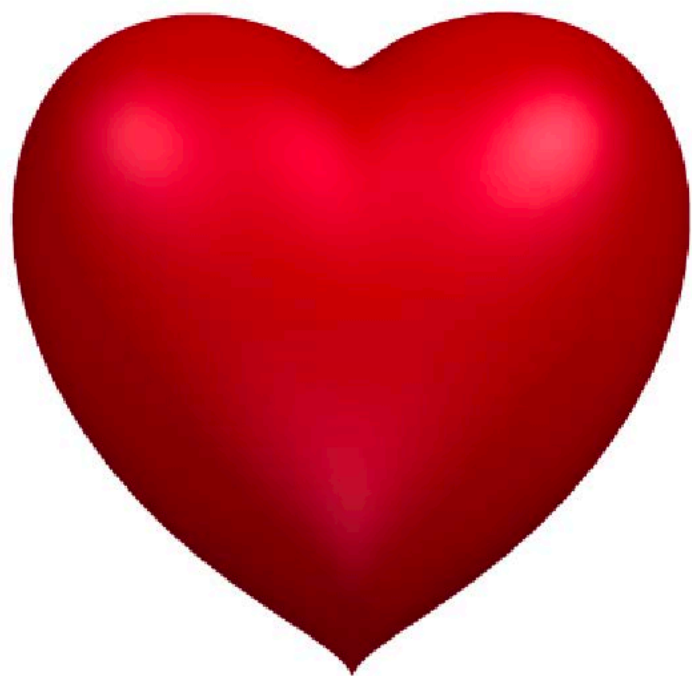

```
MandelComp = Compile[
  {{c, _Complex}},
  Module[{num = 1},
    FixedPoint[(num++; #^2 + c)&, 0, 8191, SameTest->(Re[#]^2 + Im[#]^2 >= 4 &)] ;
    num],
  CompilationTarget->"C",
  RuntimeAttributes->{Listable},
  Parallelization->True
];
```

```
Mandelbrot[x_, y_, m_] := ArrayPlot[
  MandelComp[Table[a + I b,
    {b, y - 2.7 * 2^-m, y + 2.7 * 2^-m, 0.005 * 2^-m},
    {a, x - 4.8 * 2^-m, x + 4.8 * 2^-m, 0.005 * 2^-m} (*0.002*)
  ] / 8192,
  ColorRules->{1->Black},
  ColorFunction->MandelColor,
  ColorFunctionScaling->False,
  Frame->False,
  PixelConstrained->1
];
```

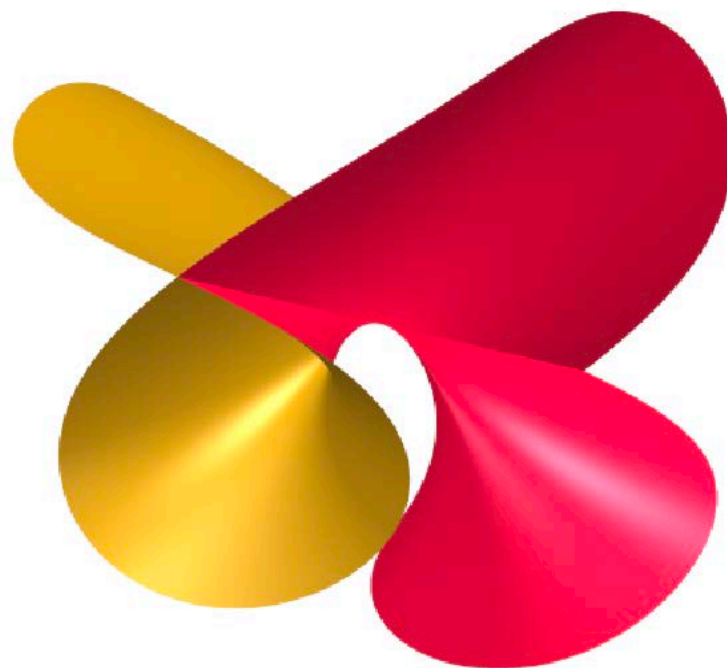





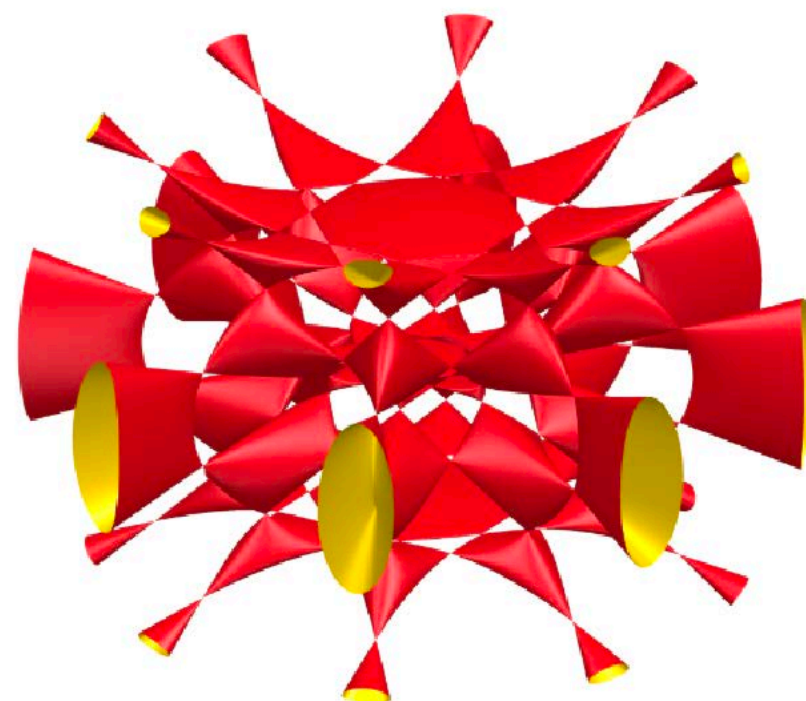
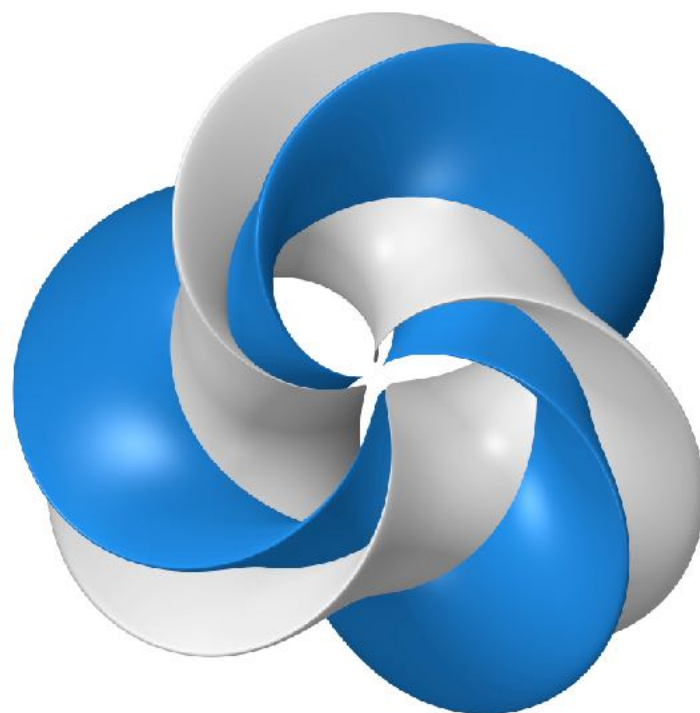
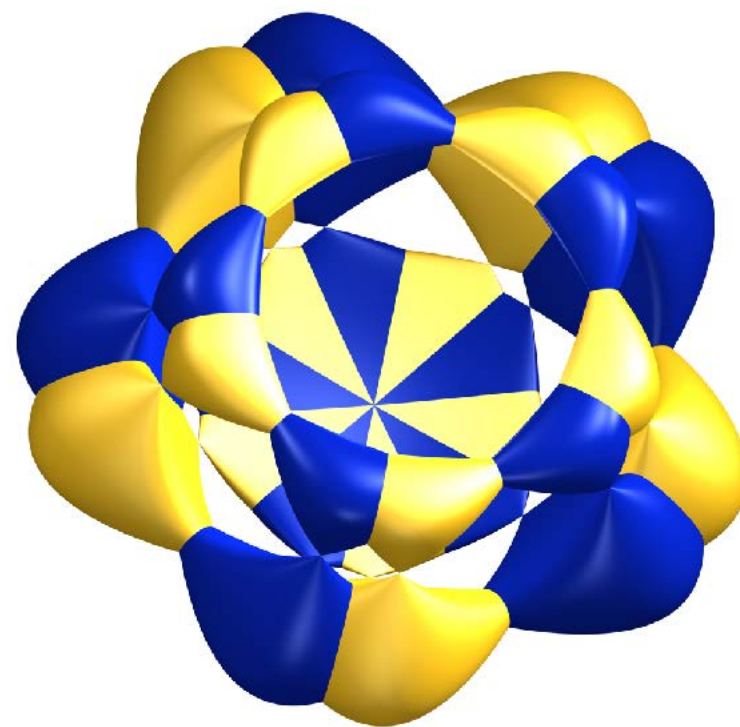




$$(x^2 + \frac{9}{4}y^2 + z^2 - 1)^3 - x^2 \cdot z^3 - \frac{9}{80}$$



$$x^3 + x^2 \cdot z^2 - y^2$$





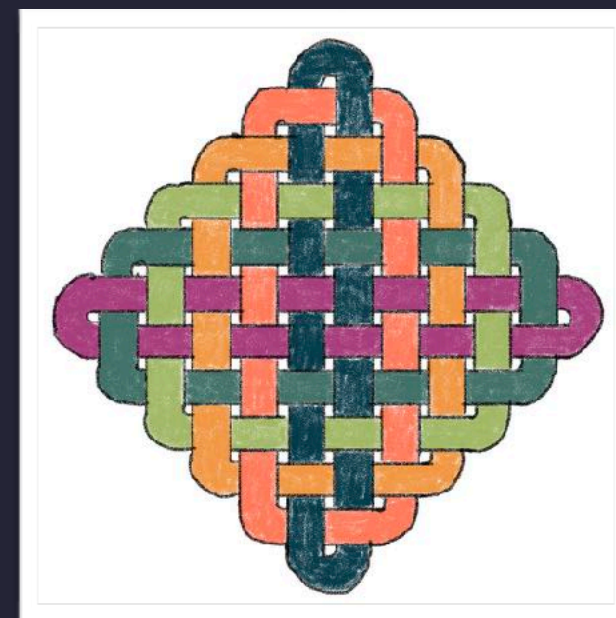
#MathArtChallenge



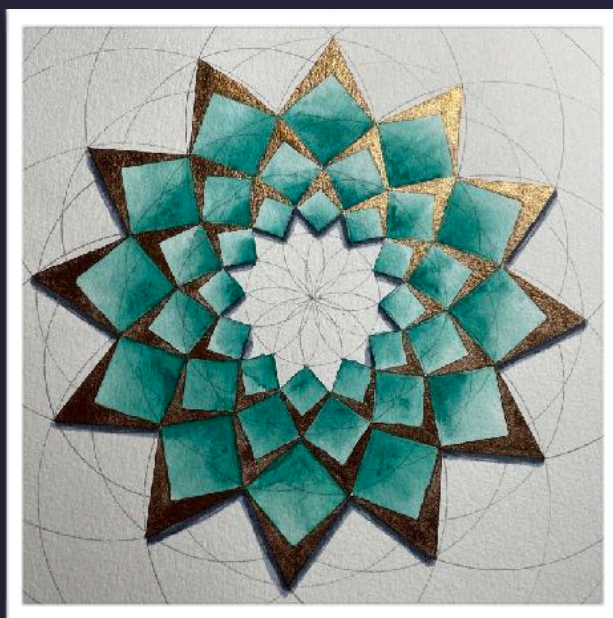
@KjerstiFried



@RosieTChen



@jayproffitt



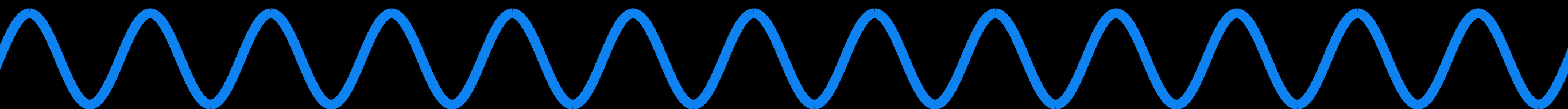
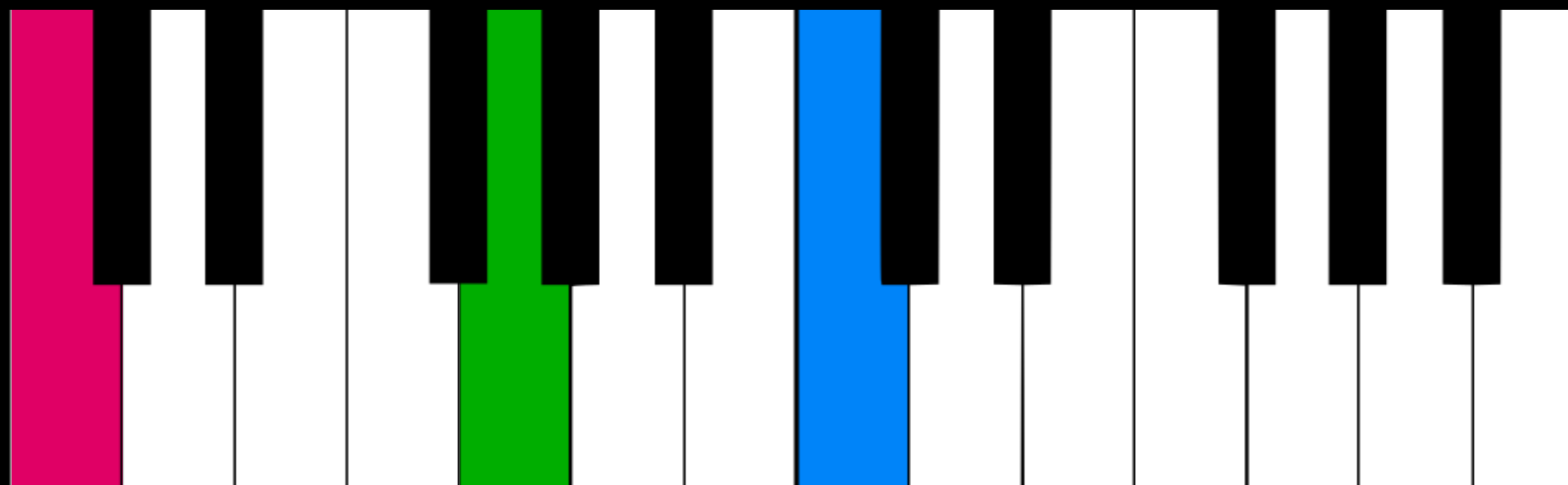
@anniek_p



@Cshearer41



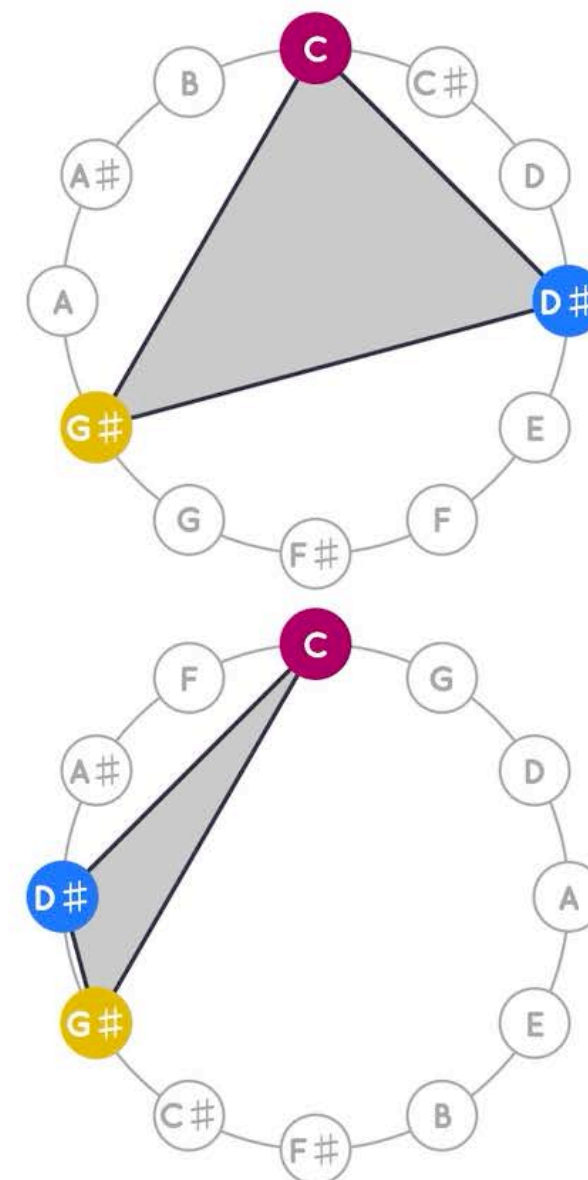
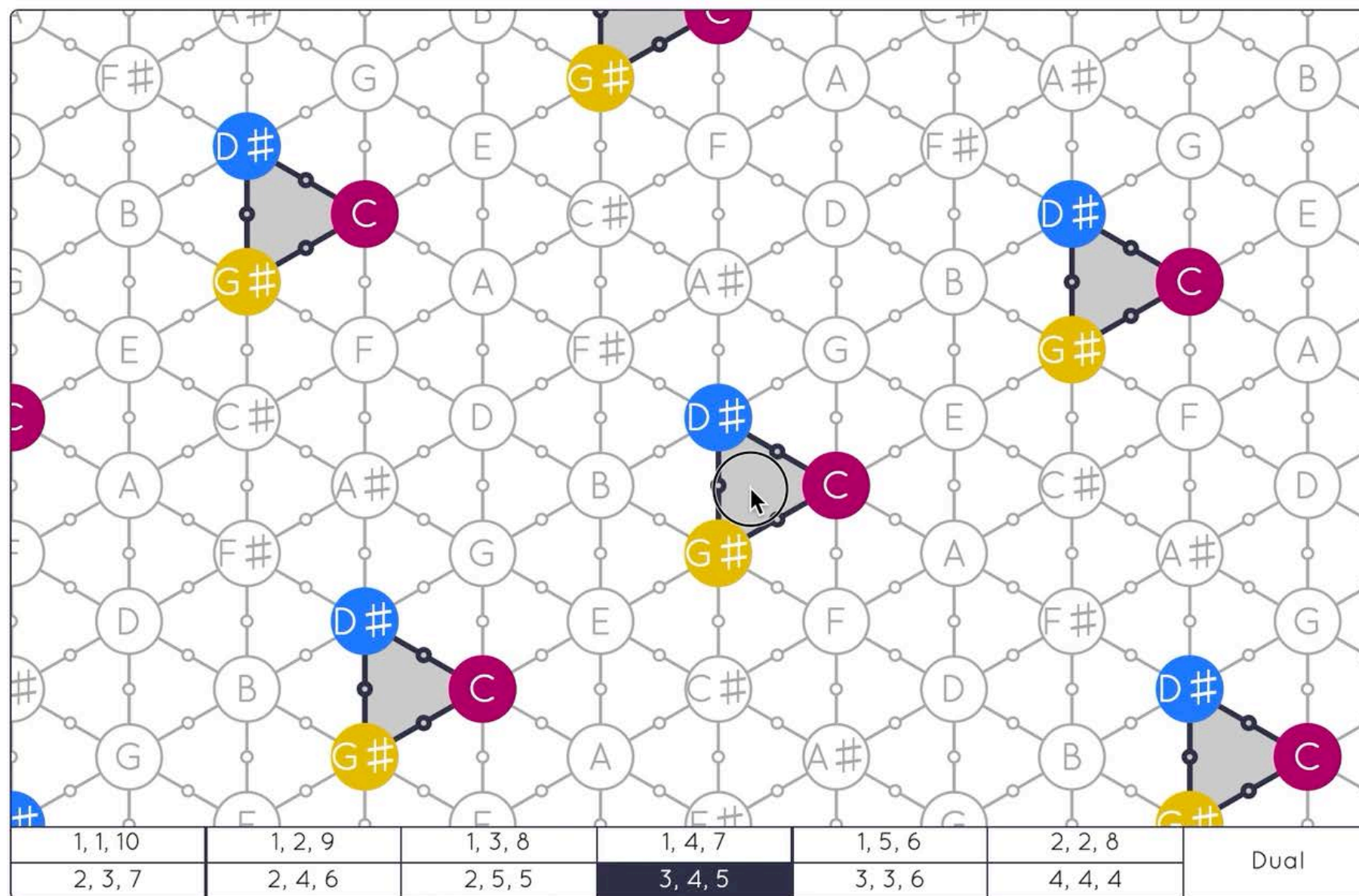
@bquentin3




$$\sqrt[12]{2}$$

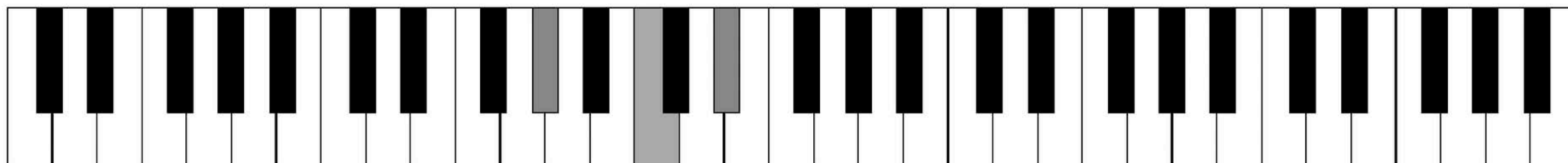
$$1.4983... \approx 1.5$$

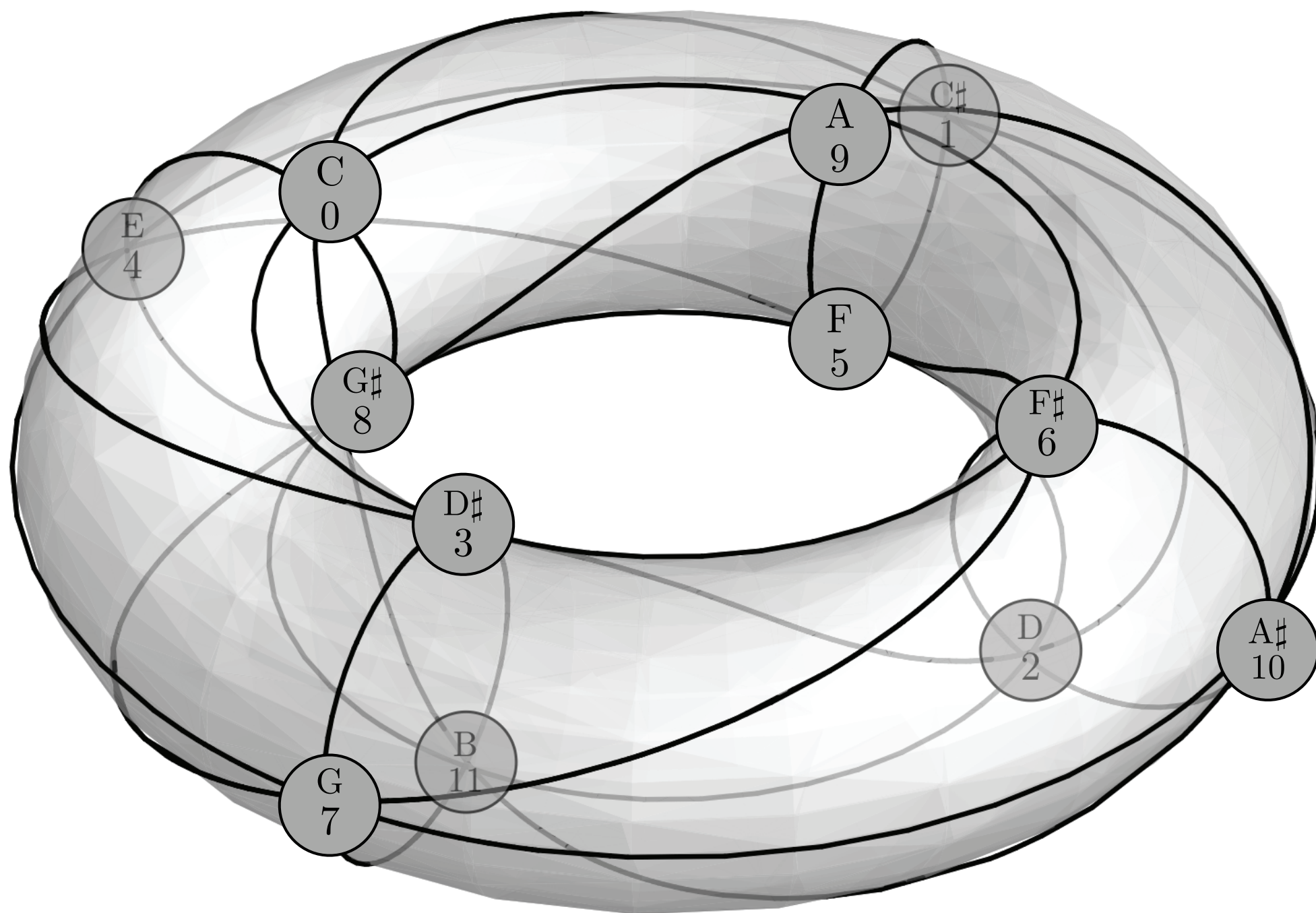




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Creativity is Problem Solving!



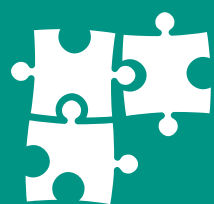
Reduce complex problems to their essentials and discover patterns.



Express situations using new or different representations.



Recognise implicit assumptions and think outside the box.



Combine tools and results from different parts of mathematics.



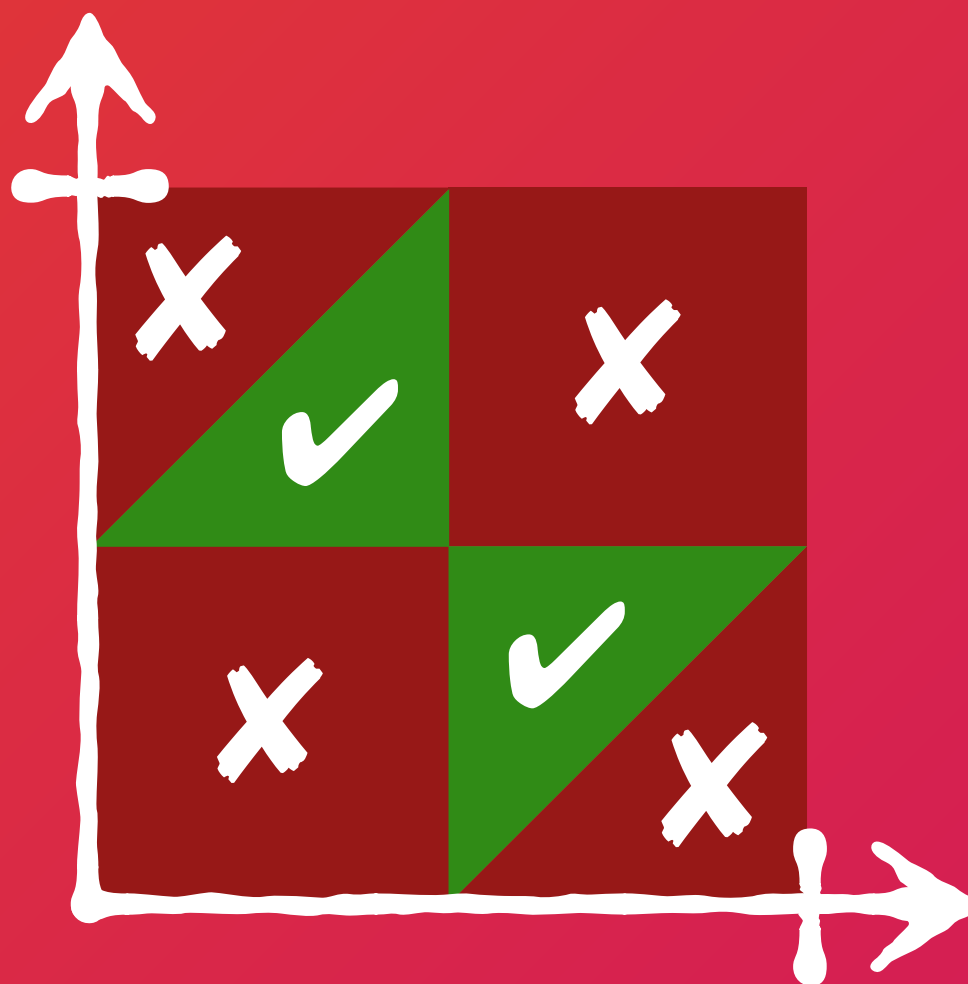
You break a stick in two different places,
uniformly at random. What is the probability
that the three resulting pieces form a triangle?



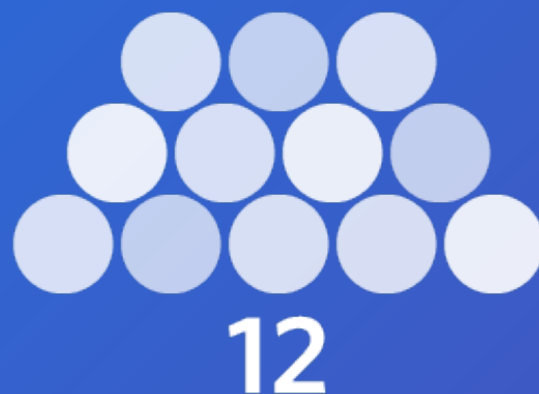
You break a stick in two different places,
uniformly at random. What is the probability
that the three resulting pieces form a triangle?



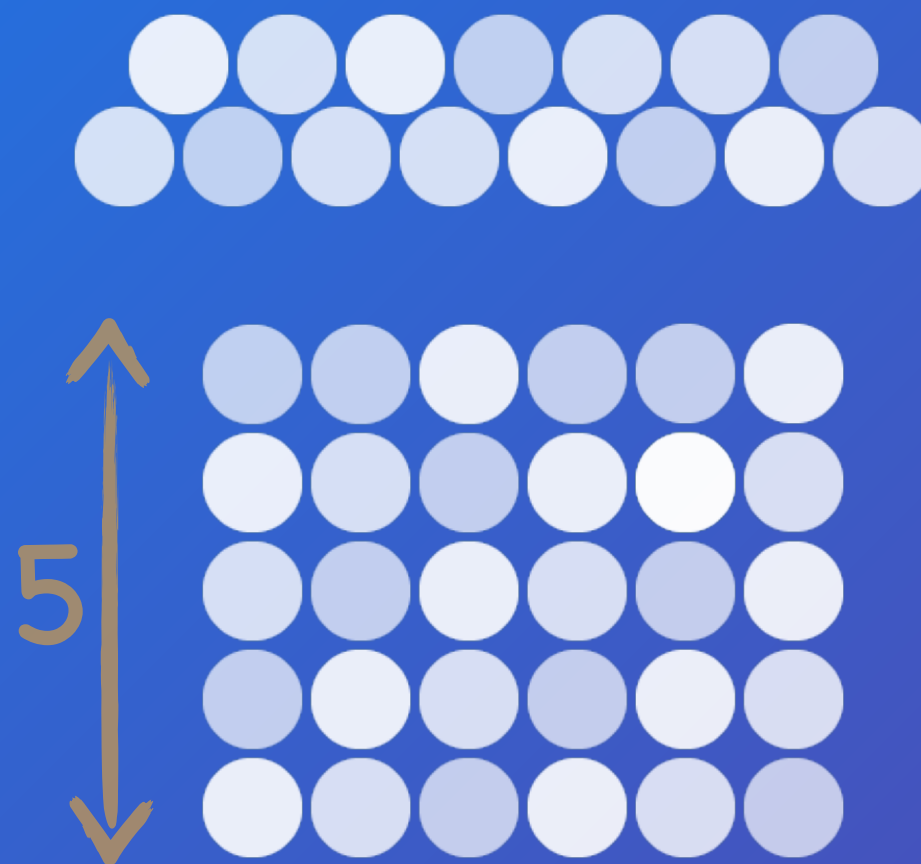
You break a stick in two different places, uniformly at random. What is the probability that the three resulting pieces form a triangle?



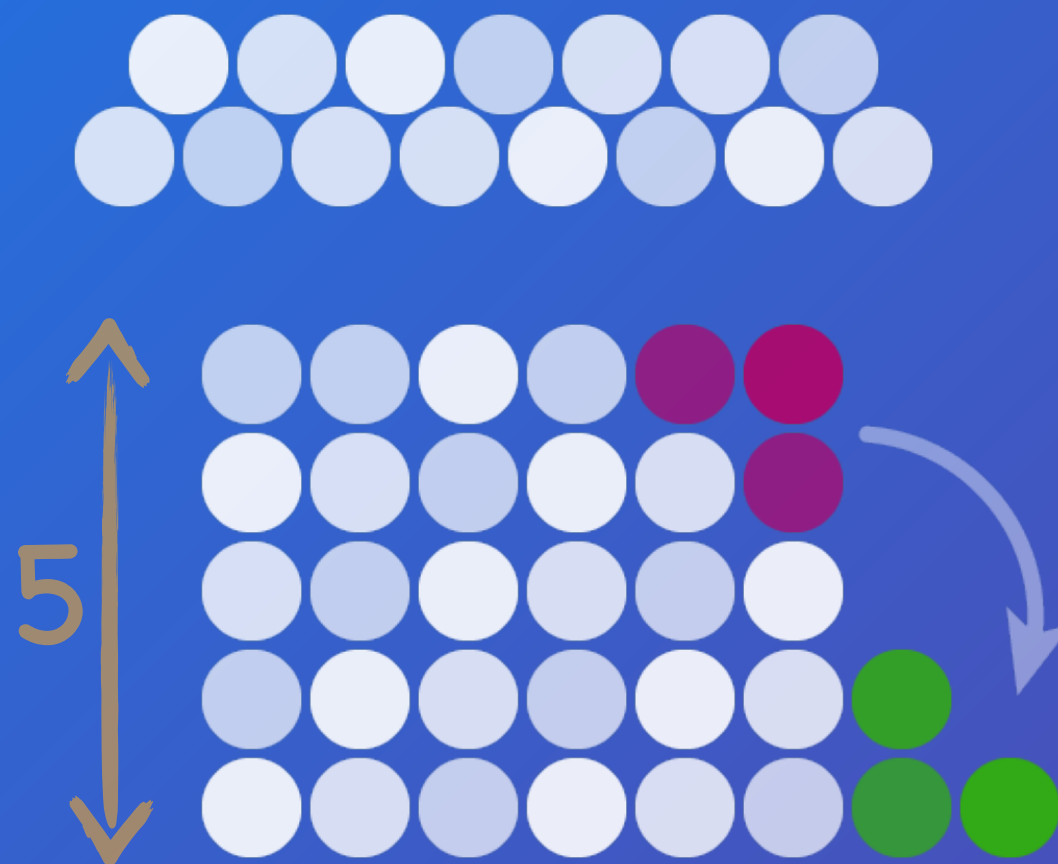
You break a stick in two different places, uniformly at random. What is the probability that the three resulting pieces form a triangle?



Here are some *Trapezium Numbers*. There is just one number between 1000 and 2000 that *doesn't* form a Trapezium. Which one?

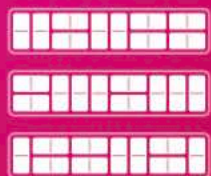


Here are some *Trapezium Numbers*. There is just one number between 1000 and 2000 that *doesn't* form a Trapezium. Which one?



Here are some *Trapezium Numbers*. There is just one number between 1000 and 2000 that *doesn't* form a Trapezium. Which one?

How many ways are there to tile a rectangle of size 2×10 with dominoes?



A semicircle lies inside a square.
What proportion of the square is shaded?

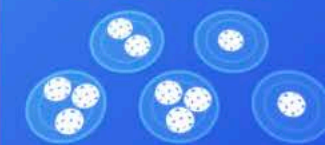
There are 20 strings in a bag. You randomly pick two ends and tie them together, until there are no free ends left. What is the expected number of loops you will create?

Rearrange these numbers and symbols to make a true equation:

2 3 4
5 + =

What is the least number of integers needed, so that any of these could be true?

How many ways are there to distribute 10 identical cookies between five different kids?



Kids don't need to receive the same number of, or any, cookies.

Can you plant 7 trees so that there are 6 straight lines containing 3 trees each?



What is the value of x ?

A castle is surrounded by a 5 meter wide, rectangular moat. Can you cross it using nothing except two planks that are 4.8 meters long?

I repeatedly toss a fair coin and record the outcome. What is the probability that the sequence "HHH" occurs before "THH"?

Every frog jumps into an adjacent square (left, right, up or down).
What is the largest number of squares that could become empty?

Can the locomotive L switch the position of the two wagons and end up where it started? Only the locomotive can fit under the bridge.

You have 10 cans of peas. All peas weigh 1 gram, except for one can with peas that weigh 0.9 grams. How often do you need to use a scale to find this lighter can?

Can you arrange the seven Tetrominoes in a 7×4 rectangle, with no gaps or overlaps?

Scientists are studying a micro-organism, starting with a single cell. Every day, each cell either splits in two (with probability p), or it dies. What is the probability that the entire organism dies eventually?

Continue this sequence:

6 10 14 15

21 22 26 33

34 35 ? ?



Three geysers A, B and C in a national park erupt every 1, 2 and 3 hours respectively. You just arrived: what is the probability that you will see geyser A erupt first?

Can you place 18 black and 18 white tiles on a 6×6 board, so that there are no "squares" with their four corners having the same colour?

What 4-digit number, when multiplied by 4, reverses its digits?

$$ABCD \times 4 = DCBA$$

What proportion of a square is closer to its centre than its edge?

Can you measure exactly 15 minutes using nothing but an 11-minute hourglass and a 7-minute hourglass?

You pick three random points on a circle. What is the probability that the resulting triangle contains the center of the circle?

This is the most efficient way to place three congruent squares in an equilateral triangle. What proportion of the triangle is shaded?



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Resources

parallel

by Simon Singh

Philipp Legner

Year 7 • Edit Account • Logout

WEEK 15
Blackboard Equation

WEEK 14
Sumaze

WEEK 13
Good Will Hunting

WEEK 12
Maths Jokes

WEEK 11
The Secret of
Happiness

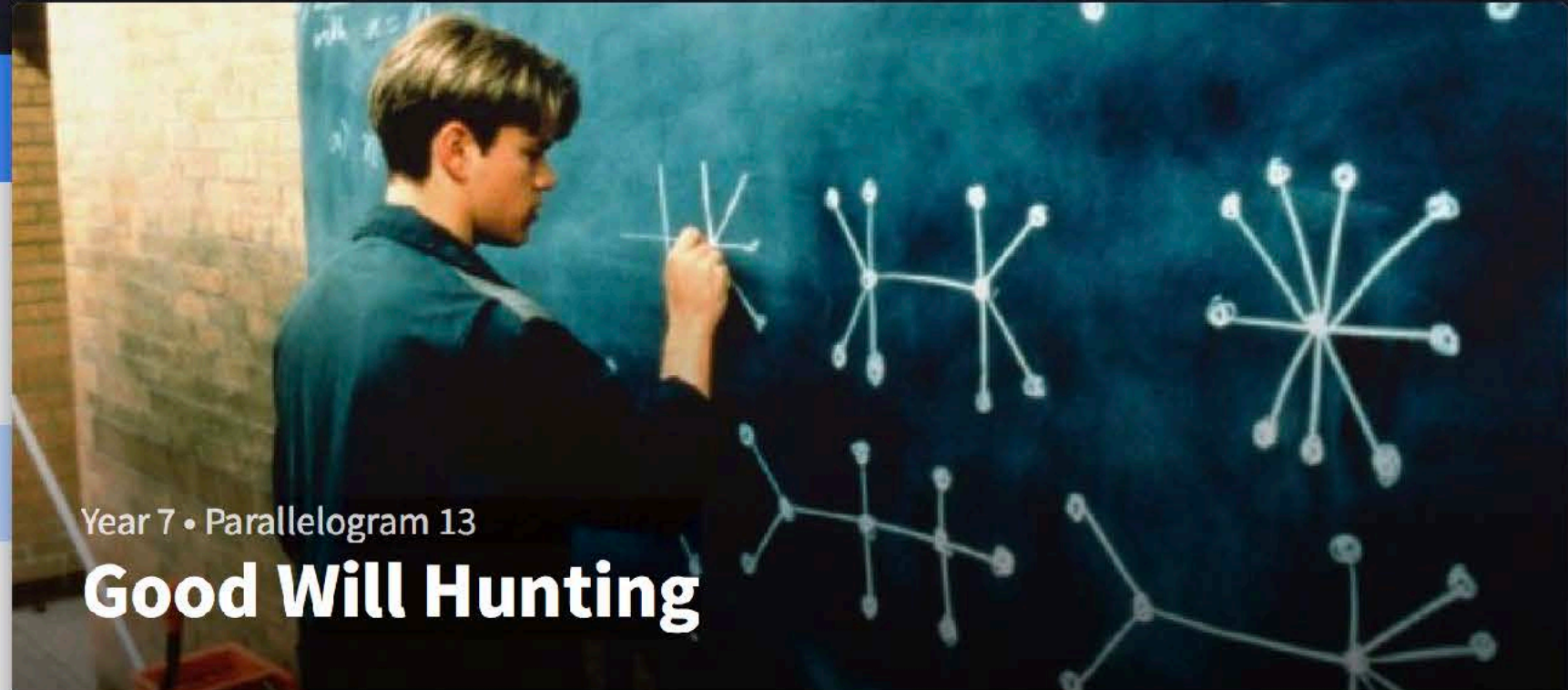
WEEK 10
A matter of factorial!

WEEK 9
Easter challenges

WEEK 8
Tricky parking problem

WEEK 7
Optimising your pizza
money

WEEK 6



Year 7 • Parallelogram 13

Good Will Hunting

Noun: Parallelogram **Pronunciation:** /ˌparəˈleləɡrəm/

1. a portmanteaux word combining parallel and telegram. A message sent each week by the Parallel Project to bright young mathematicians.

There are only 3 more Parallelograms this year, as we will be starting our summer break at half-term. If you score highly enough in the last 4 Parallelograms (#12, this one, #14 & #15) by June 1, **then you will receive a Parallel certificate**. An average of more than 40% in these four Parallelograms wins a bronze certificate, then 60% or more wins silver

Primary
Students

Secondary
Students

Early
Years

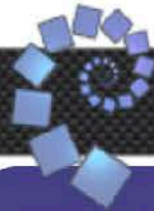
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[Secondary, Post 16 and STEP](#)

Primary Pupils



The tasks in [this feature](#) encourage you to play and explore, then think deeply about the mathematical ideas underneath.

See all problems [Open for Solution](#)
See all [Resources for ages 5-11](#)

Secondary Students



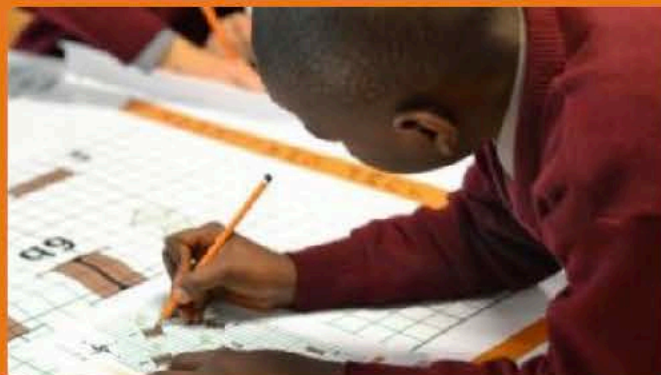
In [this feature](#), explore the problems and then try to explain what's going on!

See all problems [Open for Solution](#)
See all [Resources for ages 11-18](#)

Events and PD



Your Solutions



Tweets by @nrichmaths

NRICH maths Retweeted

Liz Woodham
[@cmw1001](#)

First day of [@nrichmaths](#) PD with a new group of primary teachers from Tower Hamlets. Six days focusing on whole class reasoning. And I get to work with [@FranMaths](#) too. Woo hoo



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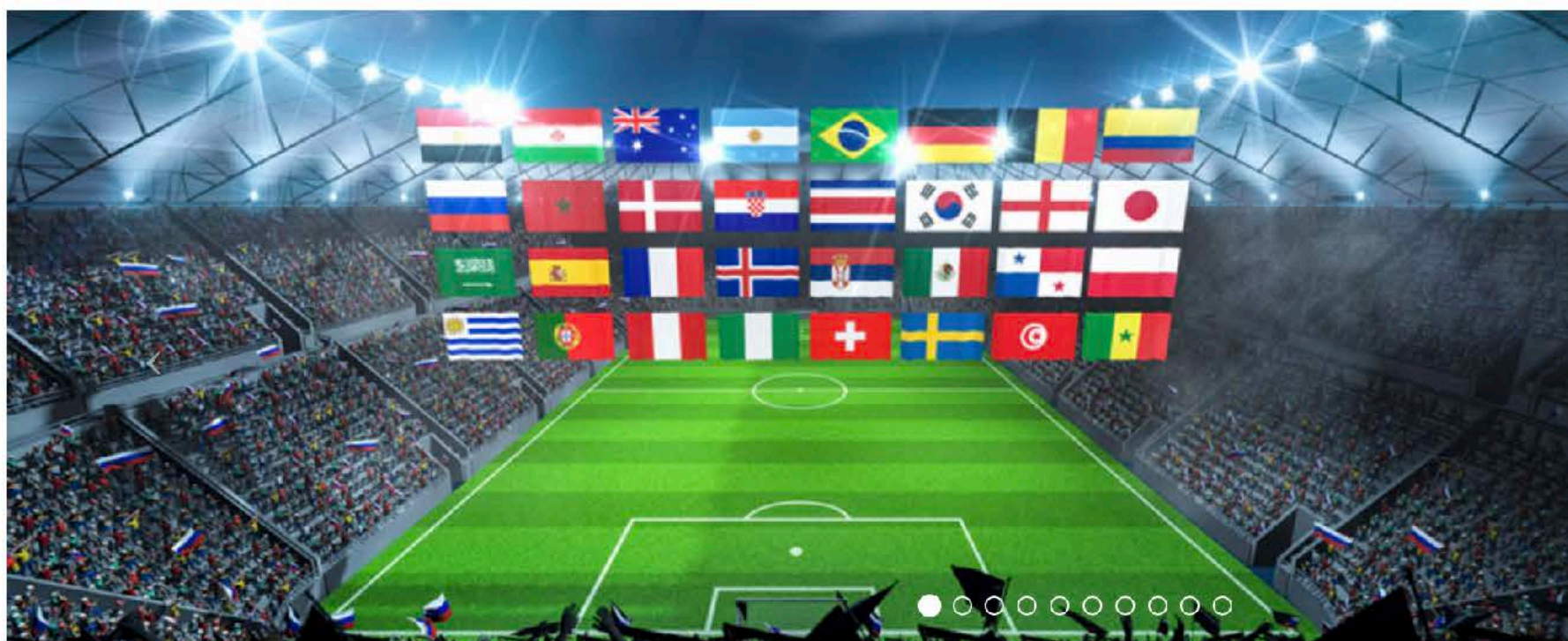
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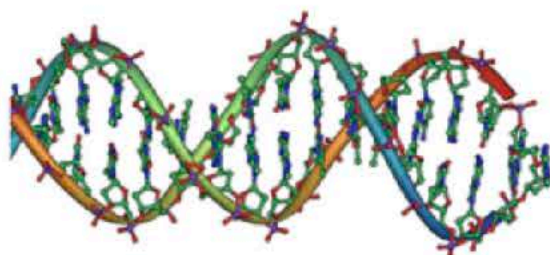
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Welcome To Plus Magazine!



Welcome to the FIFA World Cup!

From making penalties fairer or taking the perfect free kick, to designing an ideal ball and predicting results using an octopus, it's all there in our collection of football articles. Take your pick!



Genetics: Nature's digital code

Is nature using digital tools to deal with genetic information?



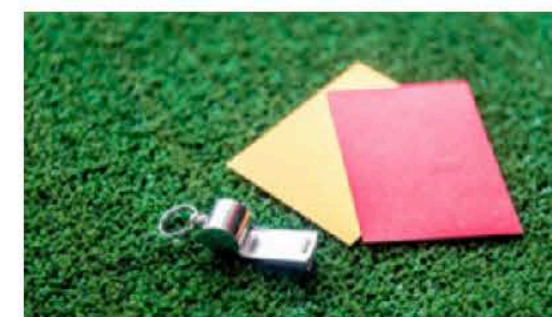
Maths in a minute: Chomp

Explore a game that involves biscuits and comes with a surprising mathematical twist — what could be better?



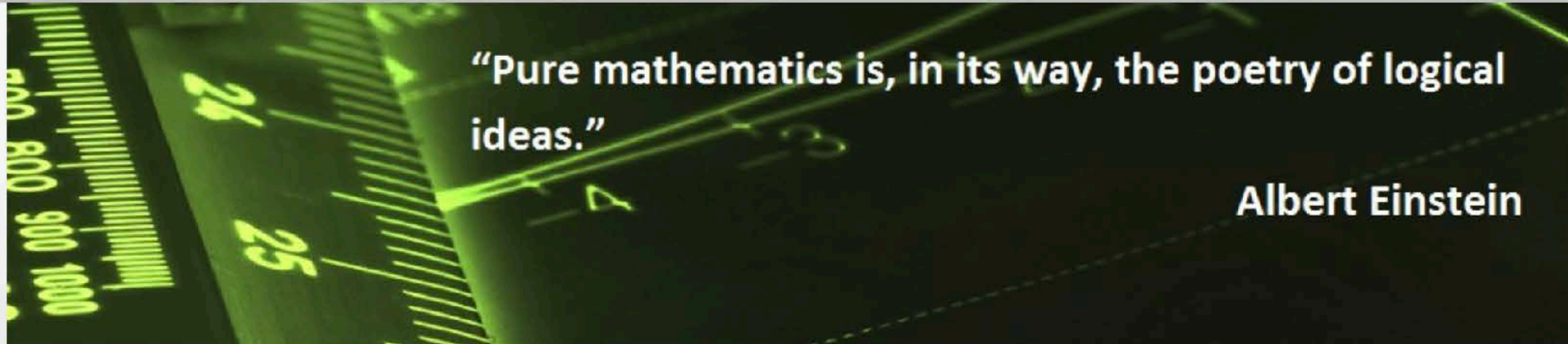
The real numbers and Cauchy sequences

We take the real numbers for granted, but what are they really? Here's an interesting way

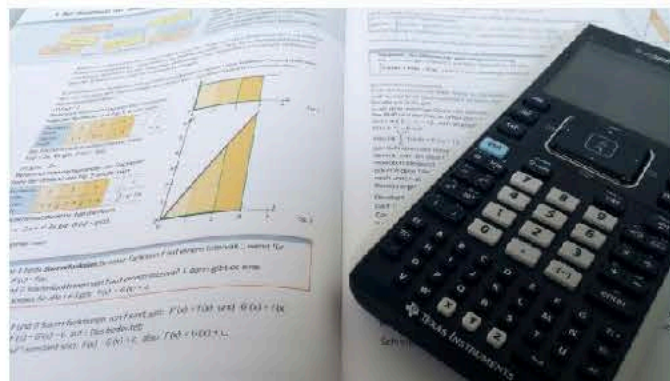


Clocking the schedule

The way many football leagues schedule their fixtures can lead to unfair effects — and unsolved maths problems! Dries



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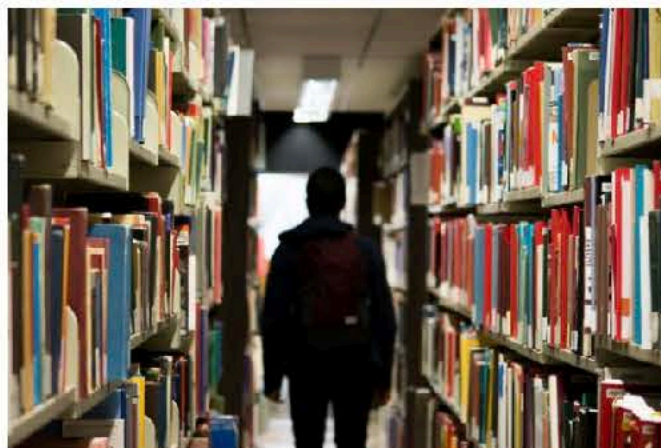


Which Degree Courses need A-level Mathematics?

A-level Mathematics is one of the most widely accepted and respected subject choices by universities. Read about how it can enhance your course options.

[Read the full](#)

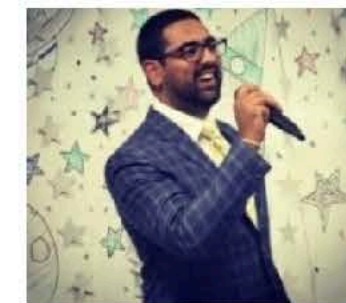
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Joint degrees including mathematics

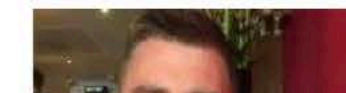
Choosing what to study at university can be hard. Lots of students choose to study joint degrees, where they study more than one subject.

Featured Profiles



Depaak Mahta - Data Scientist and Community manager

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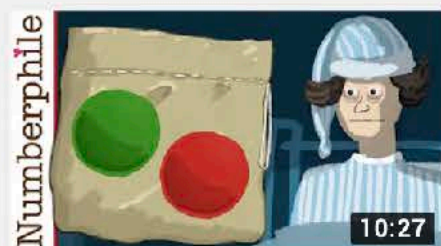
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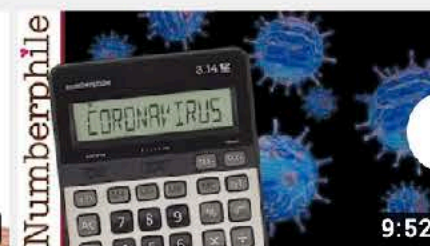
Why is this Puzzle



The Daddy of Big Numbers

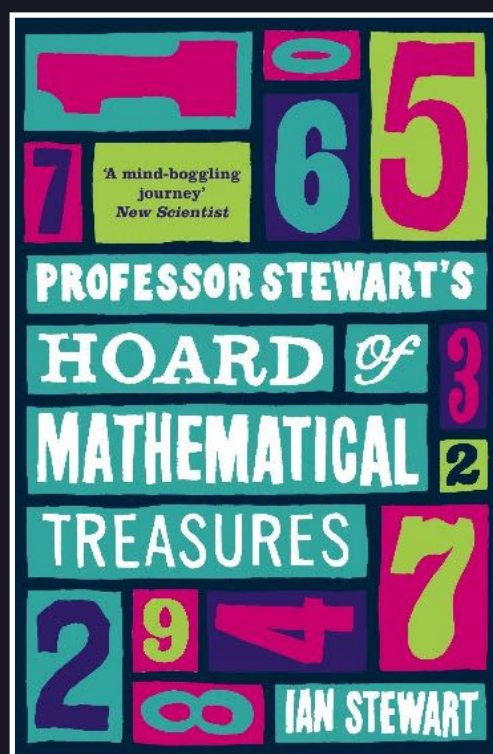


Impossible Squares -

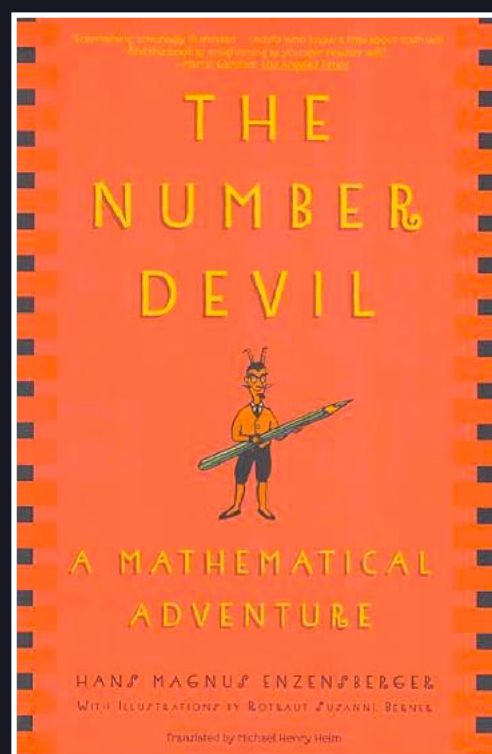


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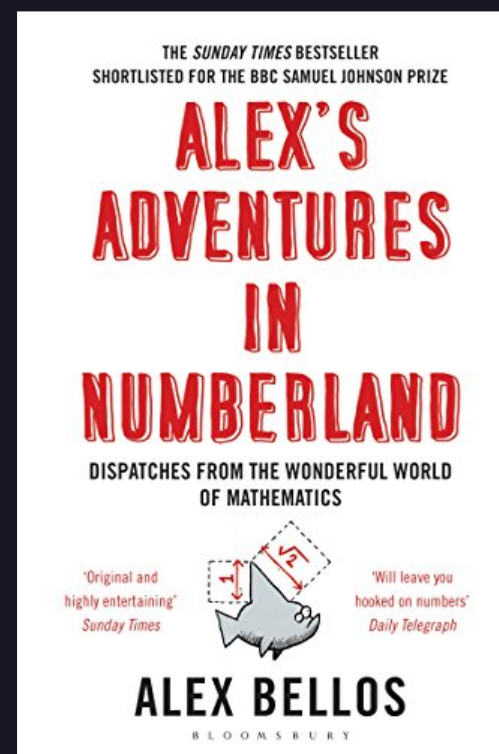
Popular Mathematics Books



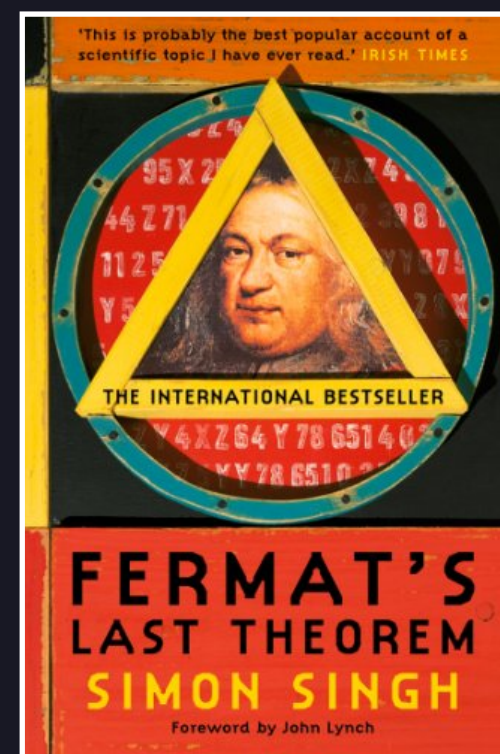
Ian Stewart



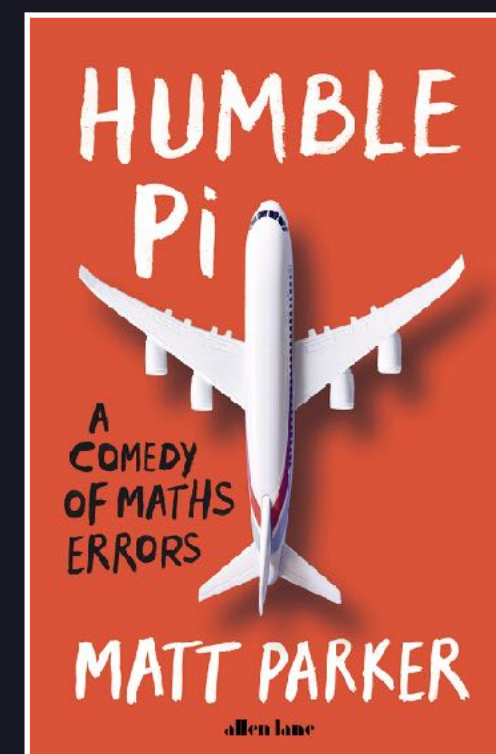
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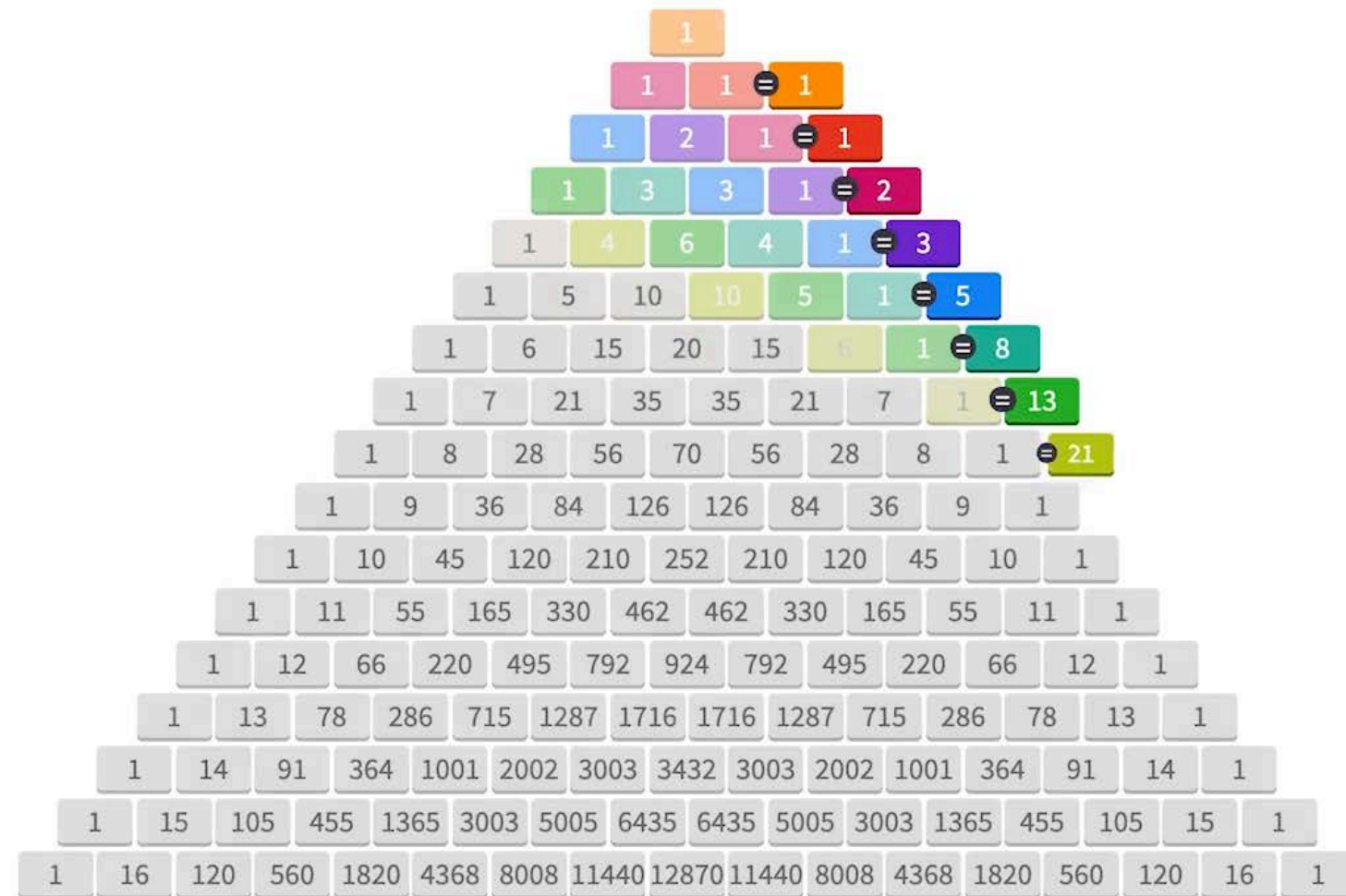
Matt Parker

Mathigon



Sequences and Patterns

- Trailer
- Introduction
- Arithmetic and Geometric Sequences
- Figurate Numbers
- Sequences as Functions
- Fibonacci Numbers
- Special Sequences
- Pascal's Triangle
- Limits and Convergence



The diagram above highlights the “shallow” diagonals in different colours. If we add up the numbers in every diagonal, we get the **???**.



Nice! 🙌



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Thanks for listening!

✉ philipp@mathigon.org

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